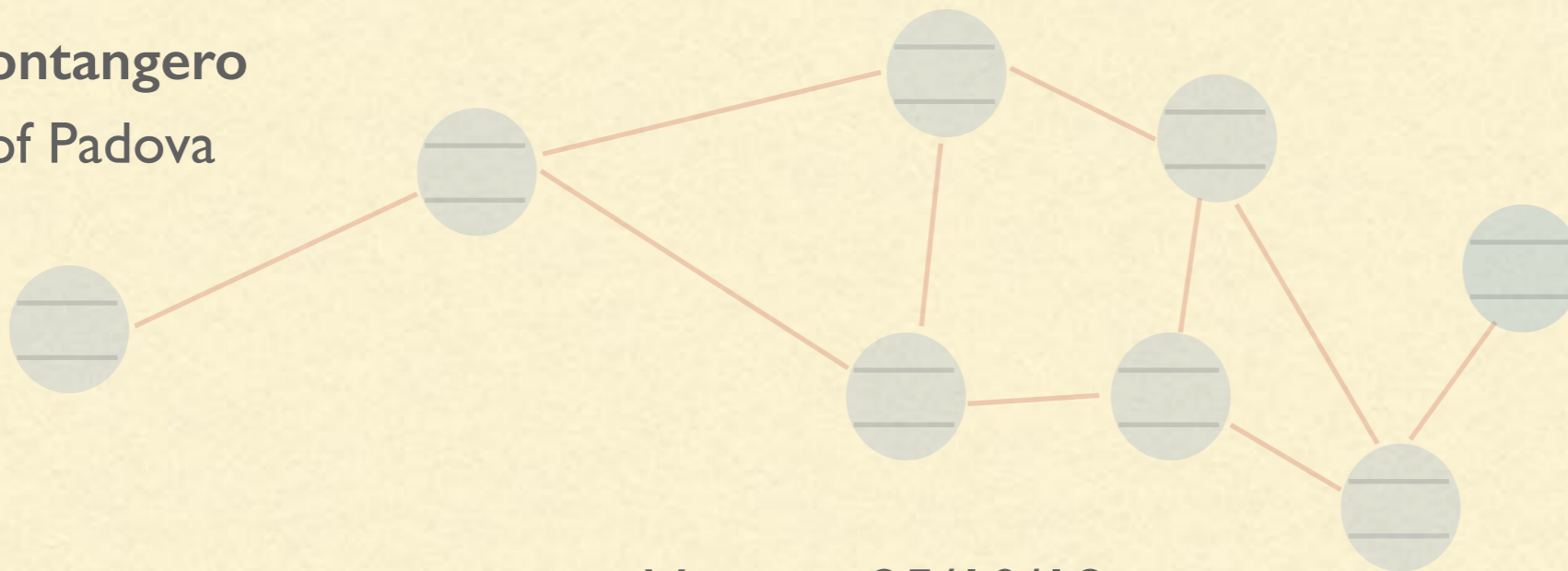


EXTREME SIMULATIONS FOR QUANTUM TECHNOLOGIES

Simone Montangero
University of Padova



Verona 25/10/18



(QUANTUM) TECHNOLOGIES

1800

1950

2000

Thermodynamics

Electromagnetism

Quantum mechanics

Quantum science

Engines

Circuits

Lasers, semiconductors..

2nd quantum
revolution

Hz

KHz

GHz

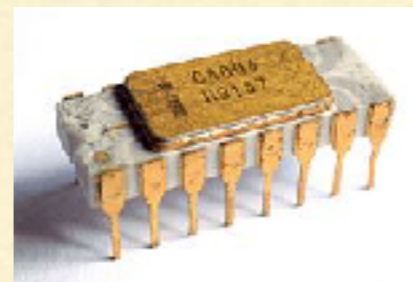
???



Babbage difference
engine



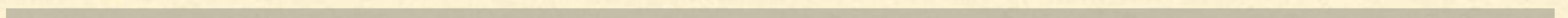
Zuse's Z3



Intel 4004

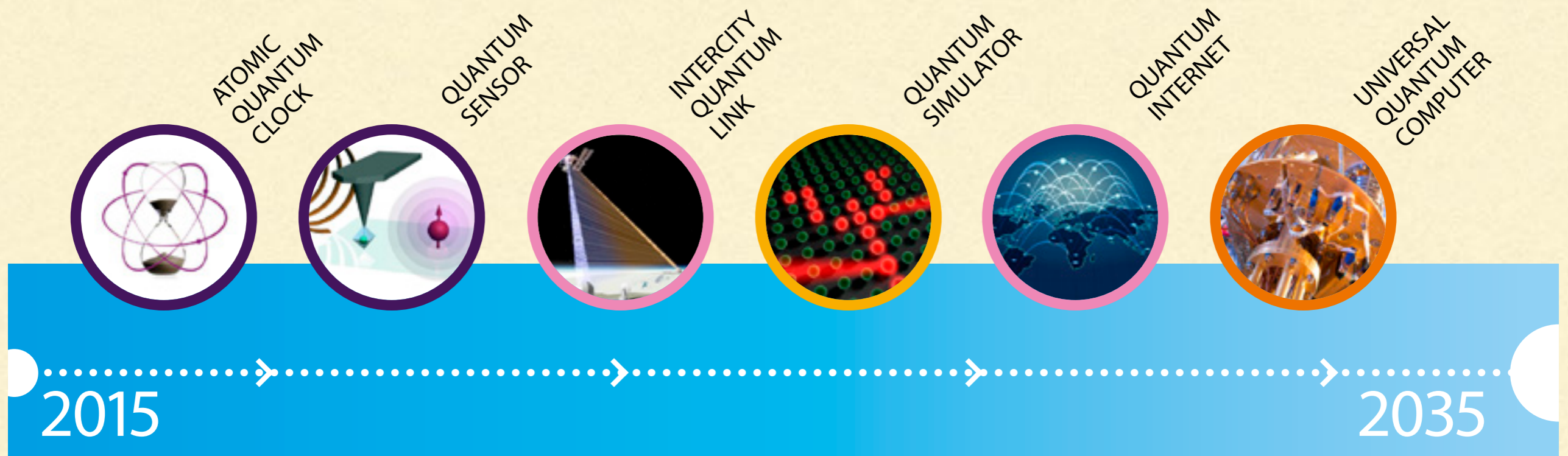
Numerical solution
of PDEs

Lattice calculations
Density Functional theory
Tensor networks...

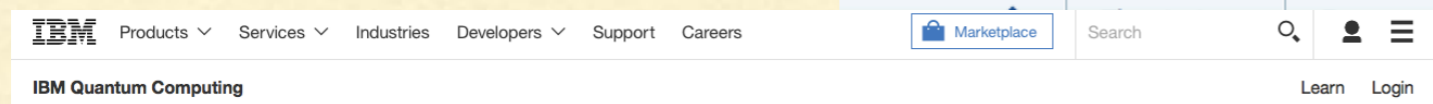
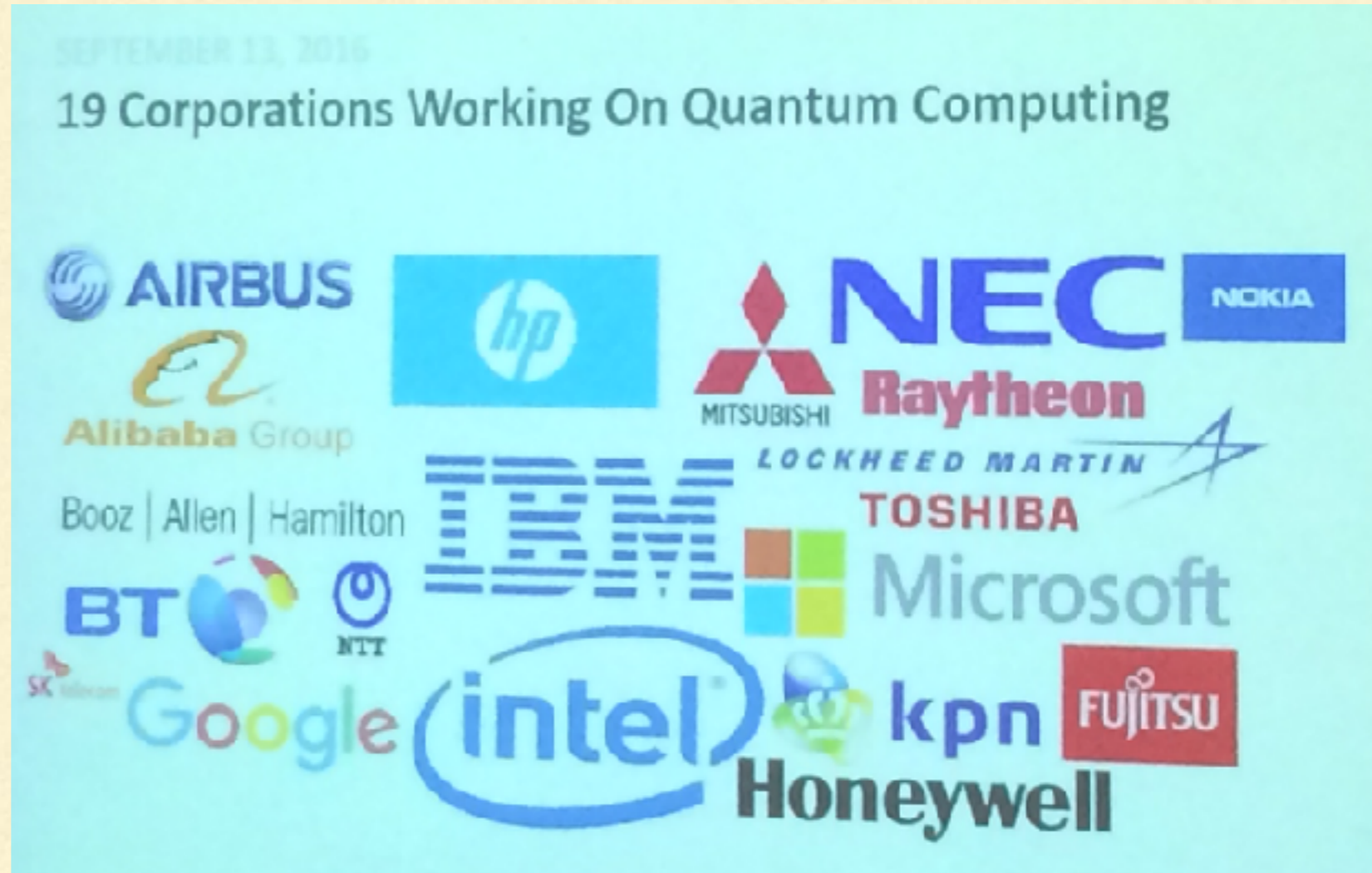
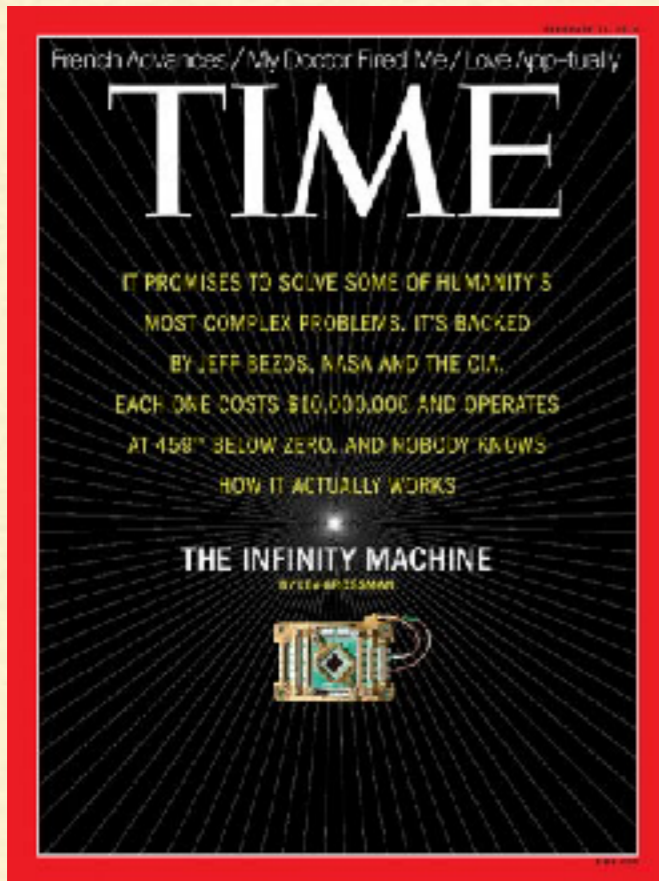


2ND QUANTUM REVOLUTION

Quantum Technologies Timeline



CURRENT EFFORTS



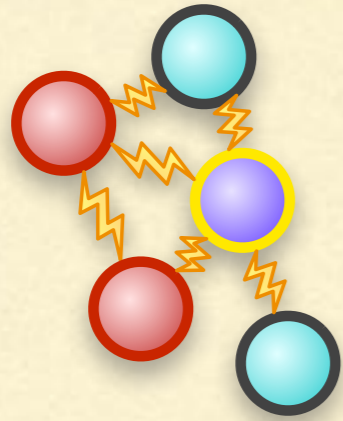
More about IBM Quantum Computing

- Demo: IBM Quantum Experience
- Quantum Computing on the Cloud
- IBM Quantum Computing Lab Tour

European Commission will launch €1 billion quantum technologies flagship

QUANTUM SIMULATORS

System



Model

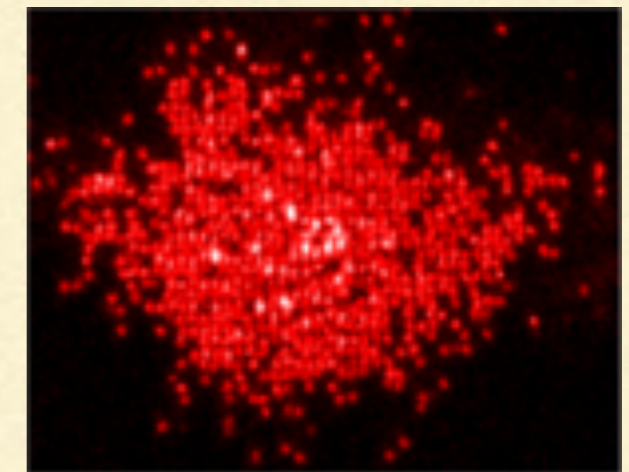
$$H = \sum \sigma_i^z \sigma_{i+1}^z + \sum_i \sigma_x$$

Energy function

Simulator



classical



quantum

- Original Feynman's motivation for QC
- Cold atoms, trapped ions, superconductors...
- Adiabatic quantum computation

CLASSICAL PROBLEMS AND AQC

Partitioning problem

For every configuration $H > 0$

$$S = \{n_1, \dots, n_N\}$$

Graph partitioning

Complete subgraph finding (clique)

If the ground state is s.t.

Is it possible to divide it in two sets
of equal value?

Binary integer programming $E_{gs} = 0$

NP-complete

Covering and packaging problems

the solution exists!

k-sat problems

Define the energy function:

If $E_{gs} > 0$

Minimal maximal matching...

$$H = A \left(\sum_{i=1}^N n_i s_i \right)^2$$

$$s_i = \{\uparrow, \downarrow\}$$

the mismatch
is minimized (NP-hard)

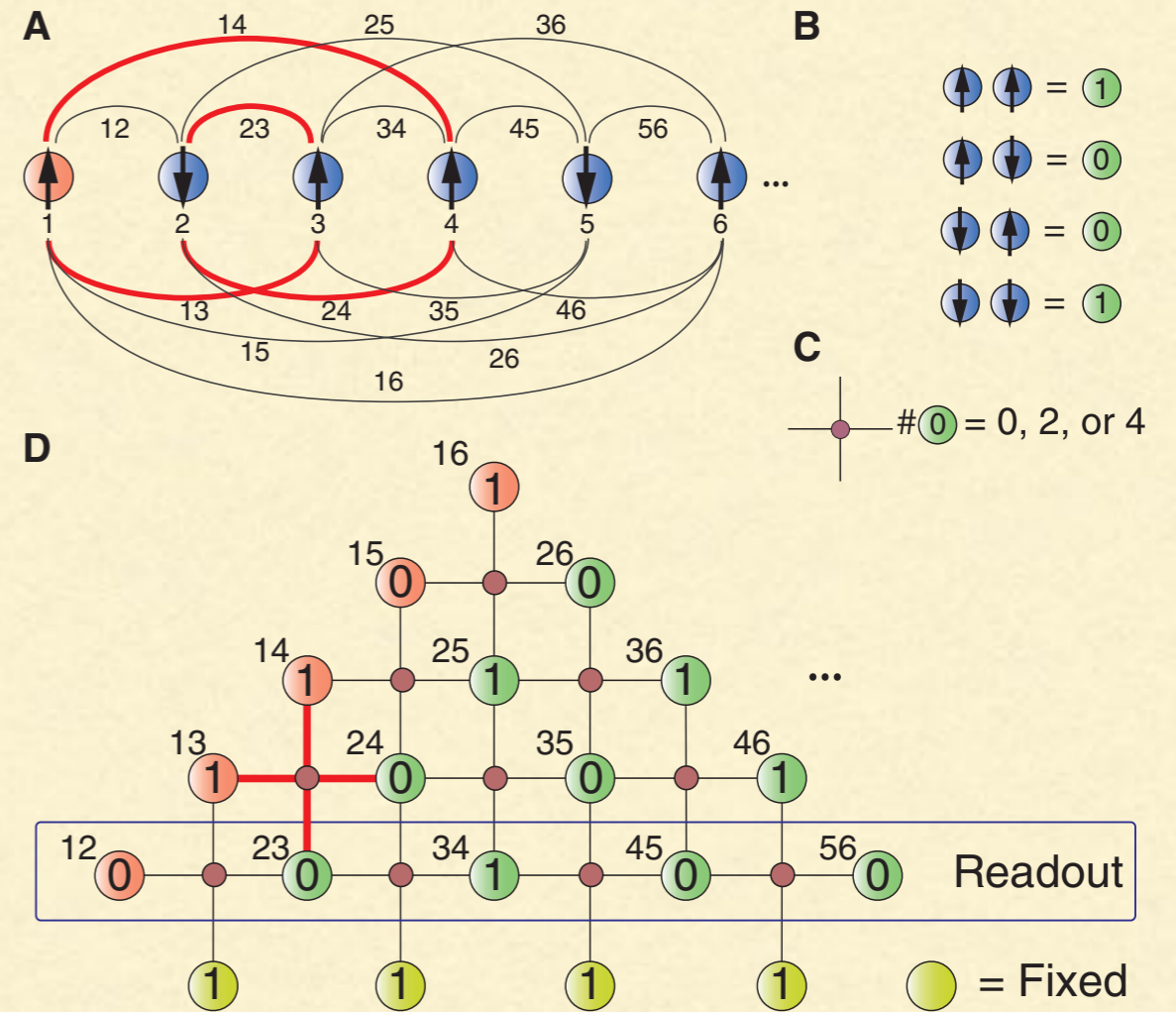
ALL-TO-ALL TO LGT MAPPING

$$H_I = \sum \sigma_x^{[k]}$$

$$H_F = \sum_{i < j} V^{[i,j]} \sigma_z^{[i]} \sigma_z^{[j]}$$

$$H_F = \sum_{k=1}^K f^{[k]} \sigma_z^{[k]} +$$

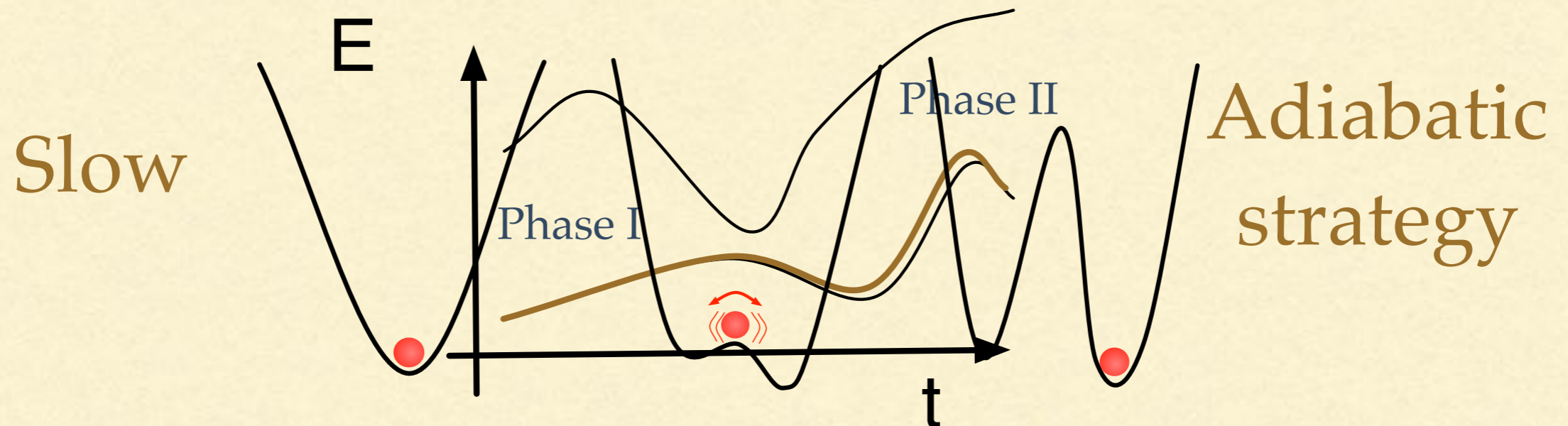
$$H_C = - \sum_{p=1}^P c^{[p]} \sigma_z^{[k_1]} \sigma_z^{[k_2]} \sigma_z^{[k_3]} \sigma_z^{[k_4]}$$



ADIABATIC QUANTUM COMPUTATION

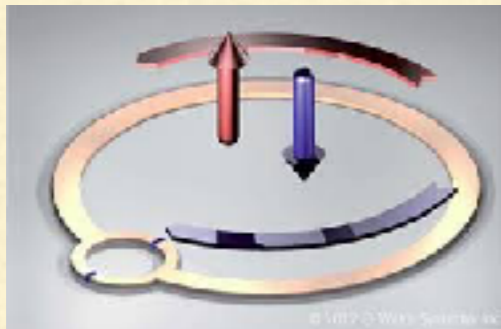
- Preparation of the system in an “easy” state ↓↓↓ . . . ↓↓↓
- Change of a system parameter to reach another ground state which encodes the problem solution ↓↑↓ . . . ↓↓↑

$$H_0 = -h_0 \sum_{i=1}^N s_i \quad s_i = \{\uparrow, \downarrow\} \quad H(t) = \left(1 - \frac{t}{T}\right) H_0 + \frac{t}{T} H_P$$



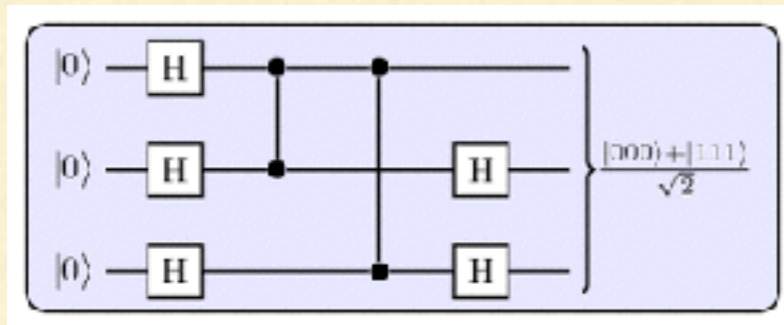
WHAT IS NEEDED?

Quantum hardware



**Validation
and
certification**

Algorithms/Protocols



Calls for:

- Classical numerical simulations
 - Optimisation
 - Software engineering
-

CHALLENGES?

System description



Control





NUMERICAL SIMULATIONS

The art of high-performance computing

MANY-BODY WAVE FUNCTION

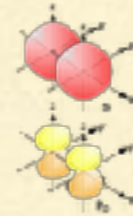
$$|\psi\rangle = \psi_0|0\rangle + \psi_1|1\rangle$$

N=1



$$|\psi\rangle = \psi_{00}|00\rangle + \psi_{10}|10\rangle + \psi_{01}|01\rangle + \psi_{11}|11\rangle$$

N=2



$$|\psi\rangle = \psi_{000}|000\rangle + \psi_{010}|010\rangle + \psi_{001}|001\rangle + \psi_{011}|011\rangle + \psi_{100}|100\rangle + \psi_{110}|110\rangle + \psi_{101}|101\rangle + \psi_{111}|111\rangle$$

N=3



$$|\psi\rangle = \psi_{0000}|0000\rangle + \psi_{0010}|0010\rangle + \psi_{0001}|0001\rangle + \psi_{0011}|0011\rangle + \psi_{0100}|0100\rangle + \psi_{0110}|0110\rangle + \psi_{0101}|0101\rangle + \psi_{0111}|0111\rangle + \psi_{1000}|1000\rangle + \psi_{1010}|1010\rangle + \psi_{1001}|1001\rangle + \psi_{1011}|1011\rangle + \psi_{1100}|1100\rangle + \psi_{1110}|1110\rangle + \psi_{1101}|1101\rangle + \psi_{1111}|1111\rangle$$

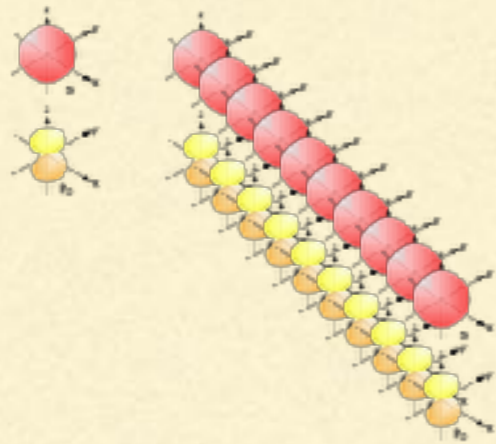
N=4



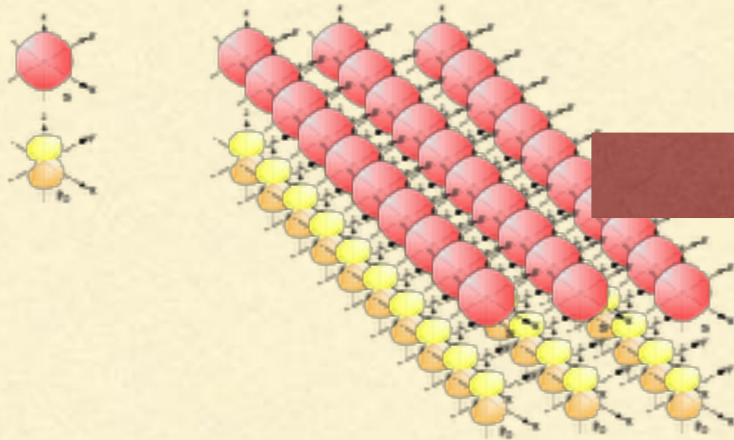
$$|\psi\rangle = \sum \psi_{\alpha_1, \alpha_2, \dots, \alpha_N} |\alpha_1, \alpha_2, \dots, \alpha_N\rangle$$

MANY-BODY WAVE FUNCTION

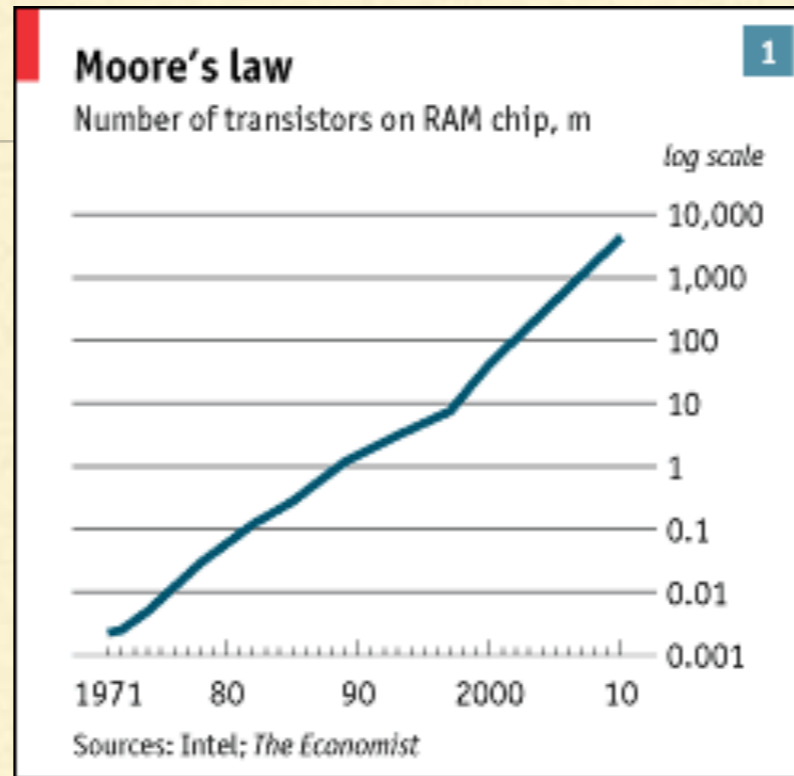
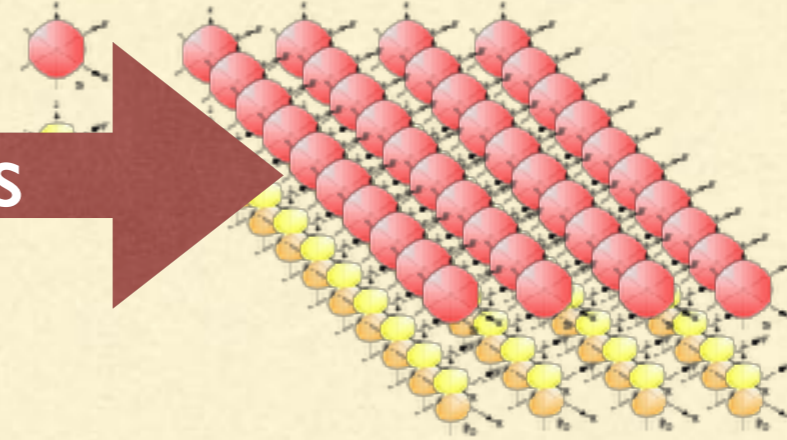
N=11



N=31



N=41



I GB

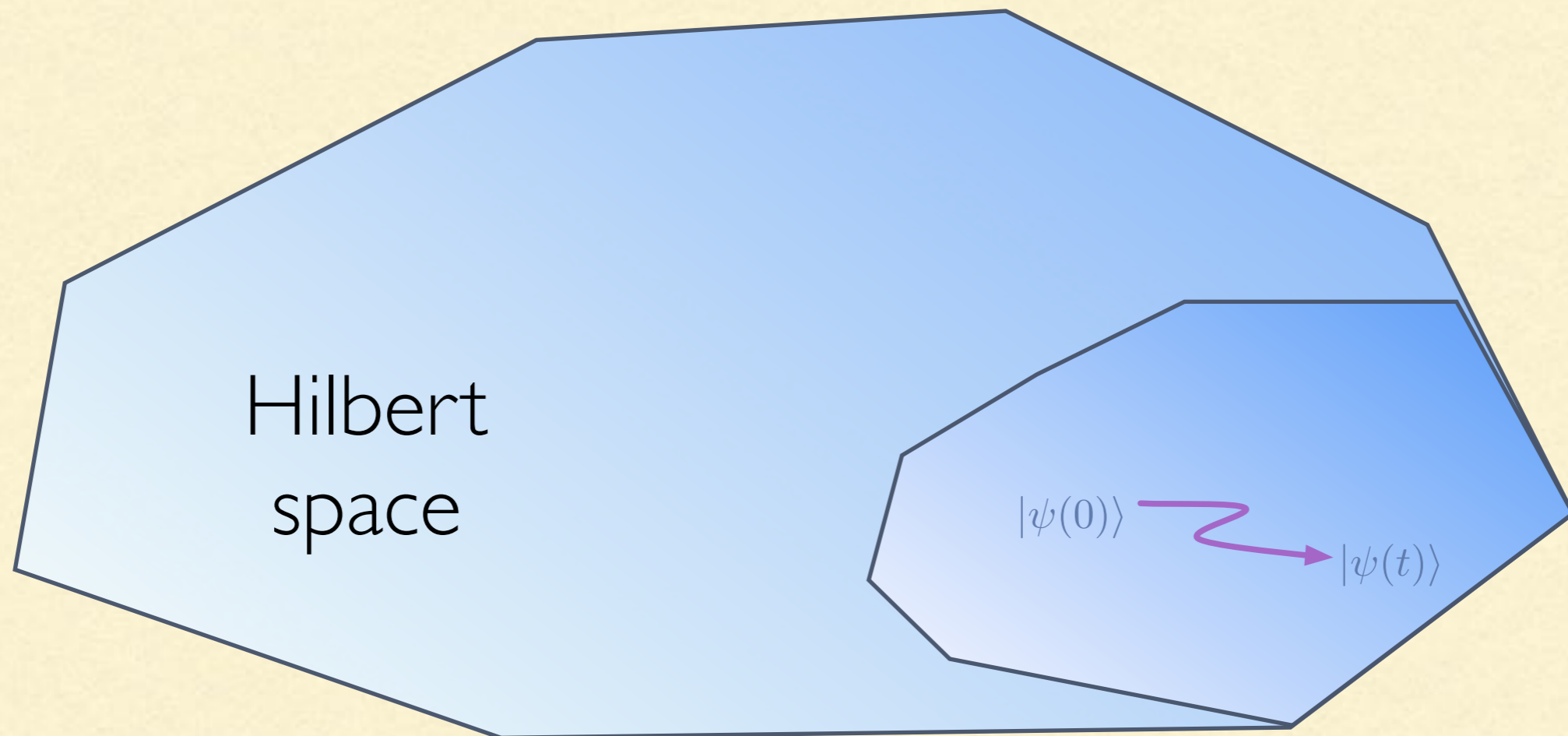
~20 years

I PB

$$|\psi\rangle = \sum \psi_{\alpha_1, \alpha_2, \dots, \alpha_N} |\alpha_1, \alpha_2, \dots, \alpha_N\rangle$$


TENSOR NETWORK STATES

“Simple” variational Ansatz to describe faithfully interesting quantum dynamics!

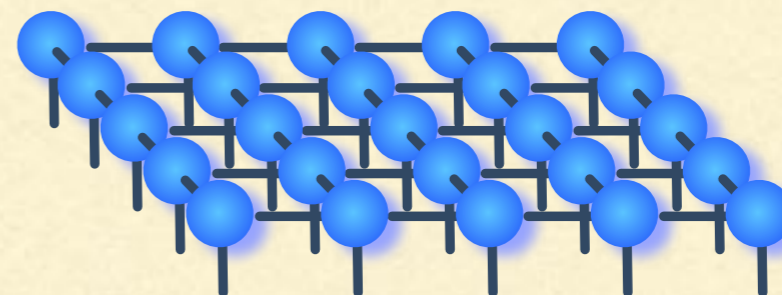


Adaptive system description tunable between mean field and exact

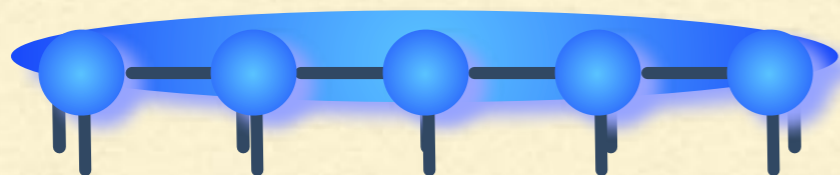
TENSOR NETWORKS

$$A_{\alpha_i}^{\beta_i, \beta_{i+1}} \equiv \text{---} \bullet \text{---}$$


$$\psi_{\alpha_1, \alpha_2, \dots, \alpha_N} \quad \mathcal{O}(d^N)$$

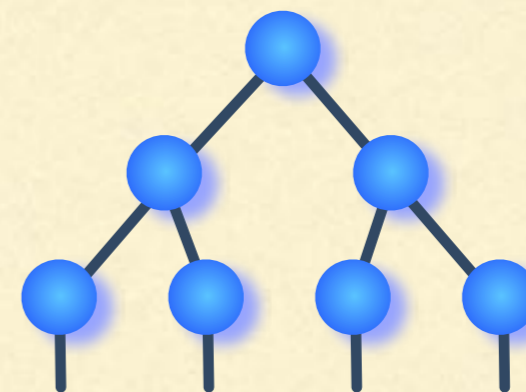


PEPS



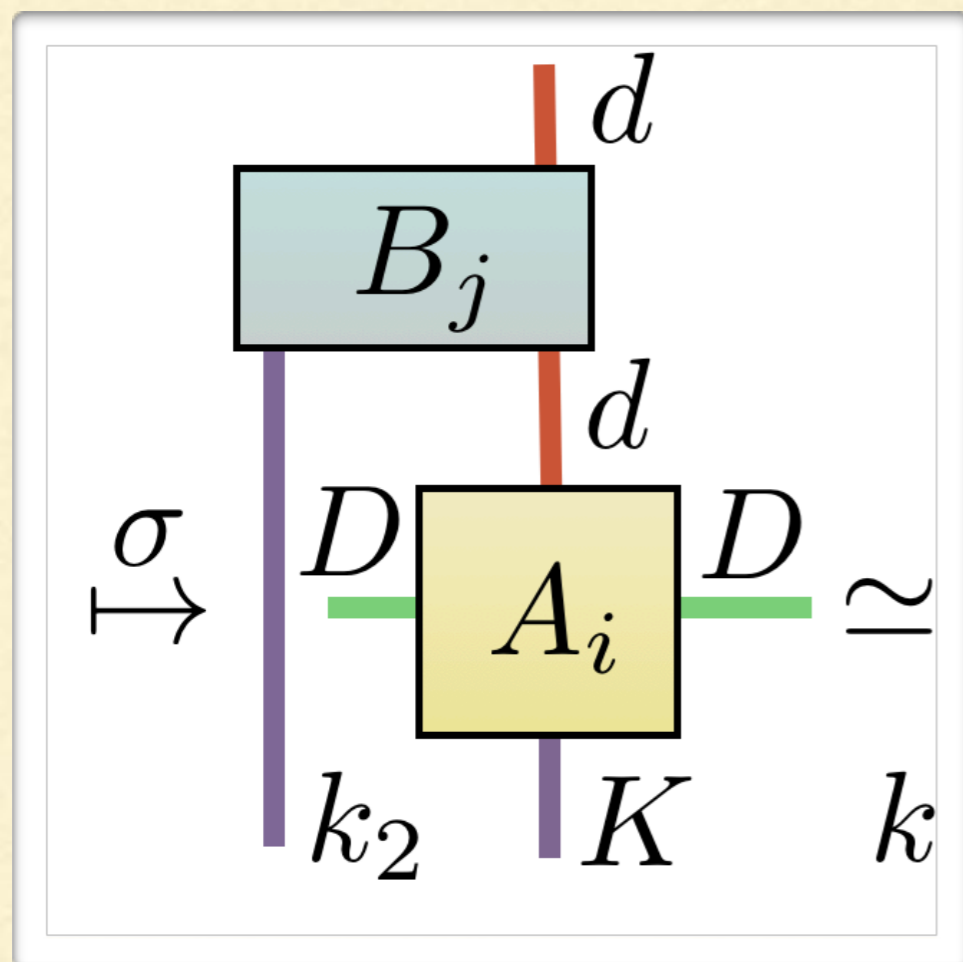
$$A_{\alpha_1}^{\beta_1} A_{\alpha_2}^{\beta_1 \beta_2} \dots A_{\alpha_N}^{\beta_{N-1}}$$

$$\mathcal{O}(Ndm^2)$$



Tree Tensor Network
(Hierarchical Tucker decomposition)

TENSOR NETWORK ALGORITHMS



- Polynomial effort (state of the art in 1D)
- No sign problem
- Works also with open system (Lindblad master equation)
- Increasingly applied in quantum chemistry
- Recently extended to Lattice Gauge Theories

GAUGE THEORIES

Theories with local symmetries (to be satisfied at every point)

CLASSICAL (electrodynamics)



$$\rho = \vec{\nabla} \cdot \vec{E}$$

QUANTUM (QED)



Gauss' law

$$\psi_x^\dagger \psi_x |\Psi\rangle = \Delta E_{x,x+a} |\Psi\rangle$$

Cirac, Lewenstein, Zoller, Verstraete, Reznik, QTFLAG...

LGT HAVE APPLICATIONS IN

High-energy
physics

QED,
QCD, ...

Condensed
matter

Quantum spin ice,
Kitaev model, ...

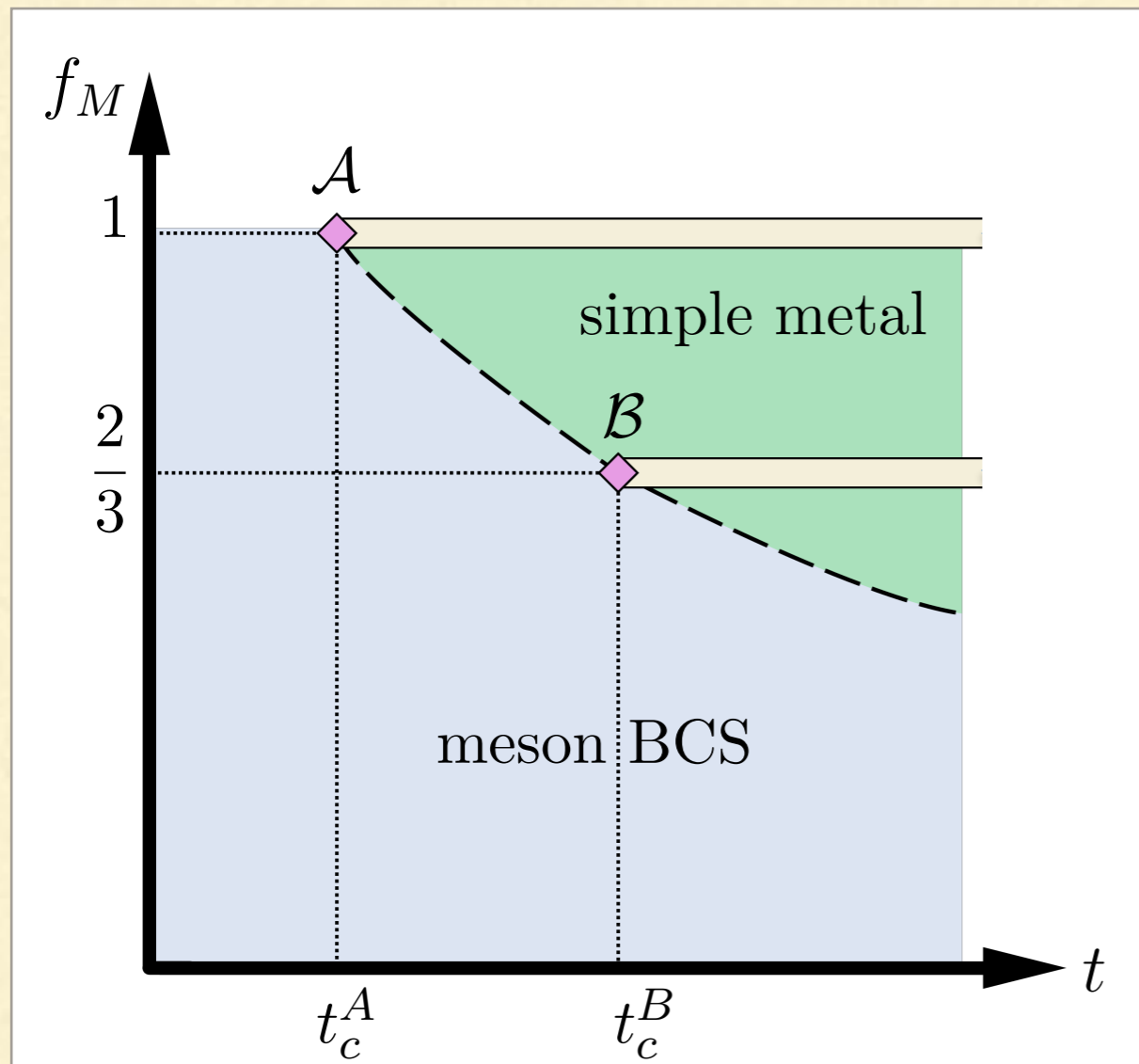
Quantum
science

Quantum
simulations, ...

Computer
science

Adiabatic
computation

SU(2) LATTICE GAUGE THEORY



$$H = H_{\text{coupl}} + H_{\text{free}} + H_{\text{break}}$$

$$H_{\text{coupl}} = t \sum_{j=1}^{L-1} \sum_{s,s'=\uparrow,\downarrow} c_{j,s}^{[M]\dagger} U_{j,j+1;s,s'} c_{j+1,s'}^{[M]} + \text{h.c.}$$

$$H_{\text{free}} = \frac{g_0^2}{2} \sum_{j=1}^L \left[\vec{J}_{j-1,j}^{[R]} \right]^2 + \left[\vec{J}_{j,j+1}^{[L]} \right]^2$$

Phase diagram at
finite chemical potential

ADDITIONAL APPLICATIONS

Tensor decomposition for Big Data and Optimization

TABLE II: Similarities and links between tensor networks (TNs) and graphical models used in Machine Learning (ML) and Statistics. The categories are not exactly the same, but they closely correspond.

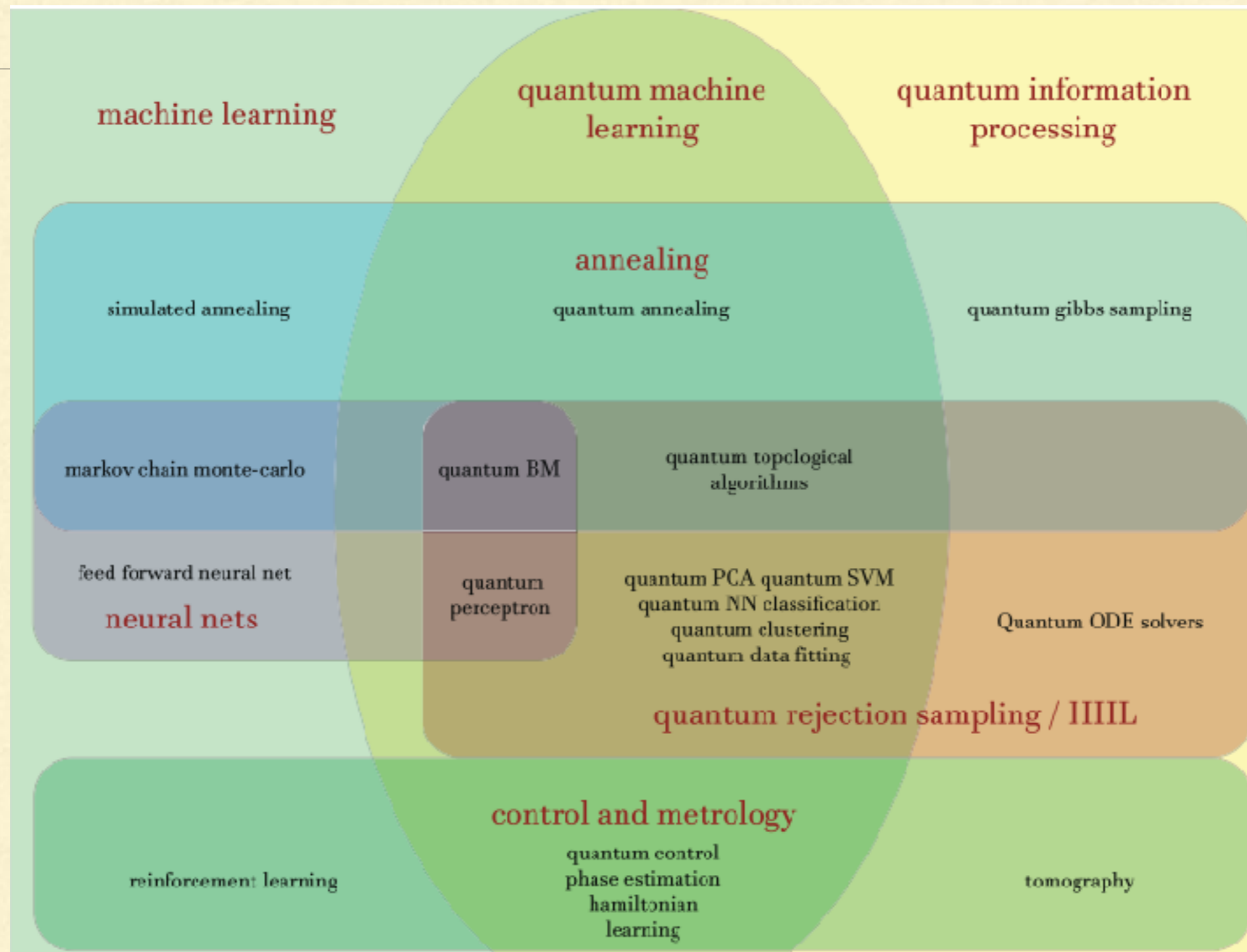
| Tensor Networks | Graphical Models in ML/Statistics |
|---------------------|--------------------------------------------------------------|
| TT/MPS | Hidden Markov Models (HMM) |
| HT/TTNS | Gaussian Mixture Model (GMM) |
| TNS/PEPS | Markov Random Field (MRF) and Conditional Random Field (CRF) |
| MERA | Deep Belief Networks (DBN) |
| DMRG and MALS Algs. | Forward-Backward Algs., Block Nonlinear Gauss-Seidel Methods |

Tensor networks for image processing



FIG. 3: Comparison of the original 512x512 8-bit grayscale image (upper-left) with images compressed with the MPS algorithm (upper-right, DCR=17.97, SSIM=0.8311, and lower-left, DCR=7.64, SSIM=0.9014) and JPEG (lower-right, DCR=33.14, SSIM=0.8311). Note how the compression artifacts are characteristic of each algorithm, even though the quality measure is the same.

QT, TN & MACHINE LEARNING



GAME OF LIFE (CONWAY'S)

Cellular automata

Two states: “dead” or “alive”

Set of simple rules that generate complexity, self-organization

Universal Turing machine

Non unitary



from wikipedia

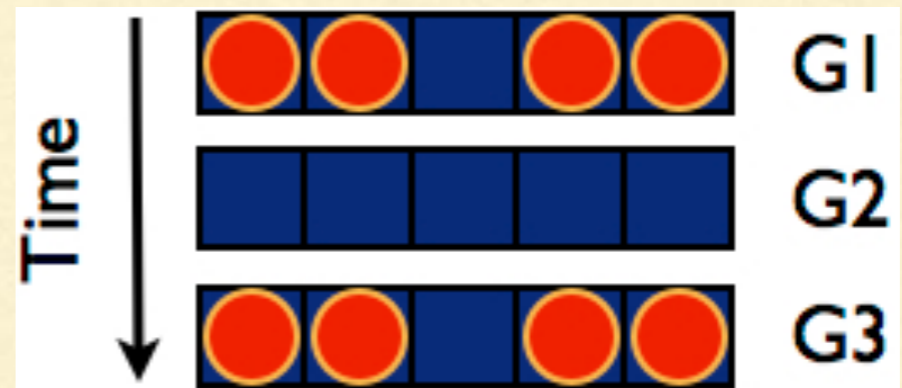
QUANTUM GAME OF LIFE

Unitary
One dimensional

$$H = \sum_{i=3}^{L-2} (b_i + b_i^\dagger) \cdot (\mathcal{N}_i^3 + \mathcal{N}_i^2)$$

$$\mathcal{N}_i^2 = \sum_P n_\alpha n_\beta \bar{n}_\gamma \bar{n}_\delta$$

$$\mathcal{N}_i^3 = \sum_{P'} n_\alpha n_\beta n_\gamma \bar{n}_\delta$$



Blinker

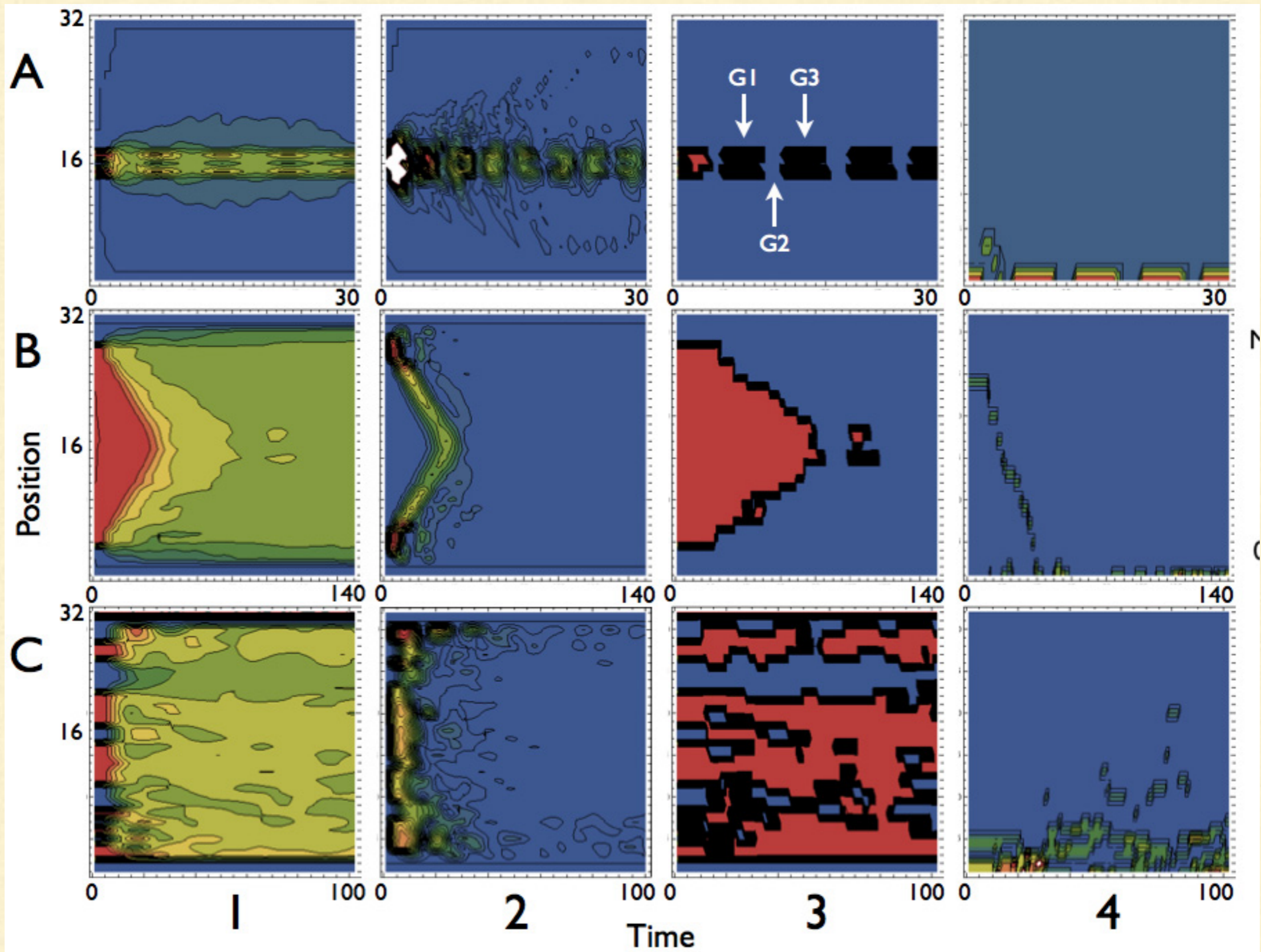
Two possible states:
“active only if surrounded by 2 or 3 alive sites”

Population

Activity

Discrete Pop.

Clustering





OPTIMAL CONTROL

Steering quantum systems at your will

Classical OCT problem



+



=



+



?
=



Quantum OCT problem

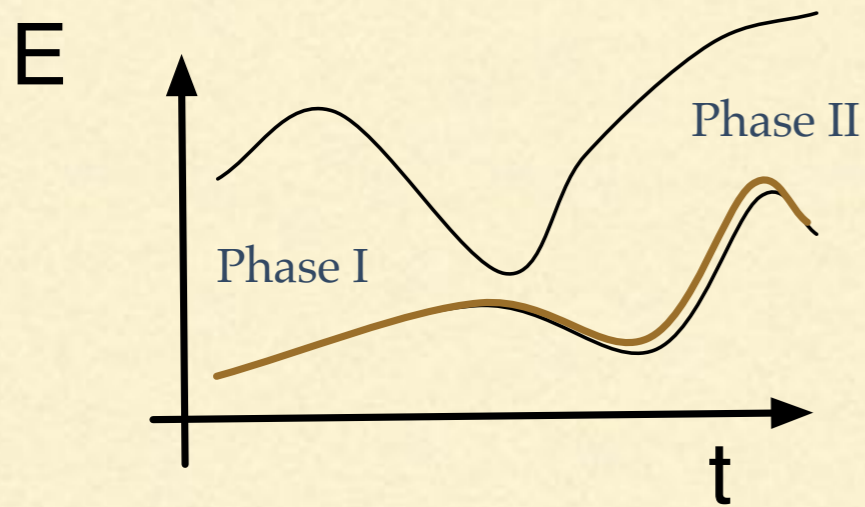
QUANTUM OPTIMAL CONTROL



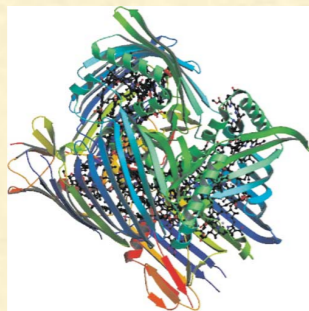
$$i\frac{\partial}{\partial t}|\psi(t)\rangle = (H_0 + f(t)H_1)|\psi(t)\rangle \quad \min_{f(t)} J(|\psi(T)\rangle)$$

- Few-body: standard optimal control
(high-accuracy, many iterations, complete knowledge...)
- Many-body: dCRAB
(high-efficiency, few iterations, minimal knowledge...)

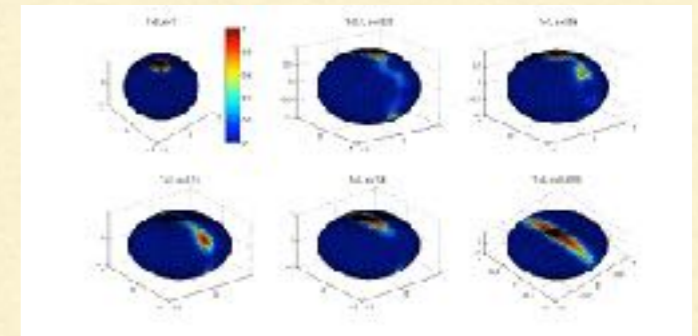
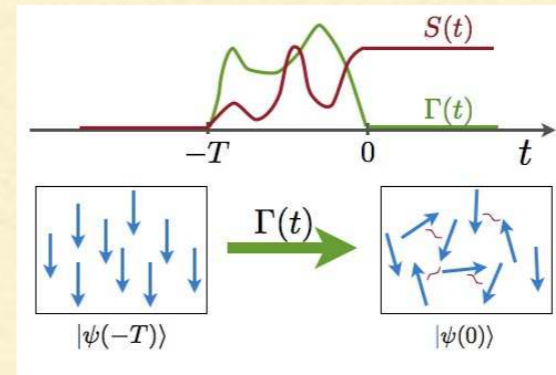
APPLICATIONS



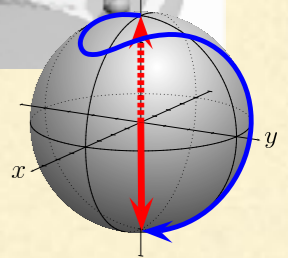
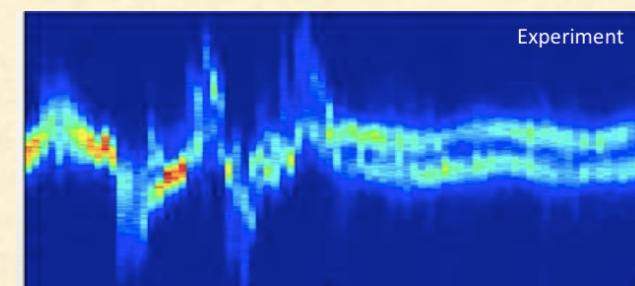
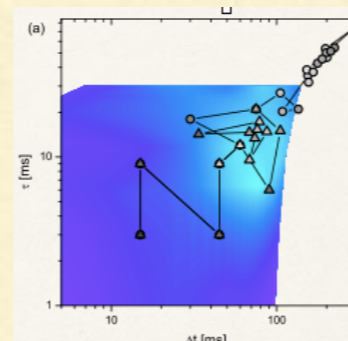
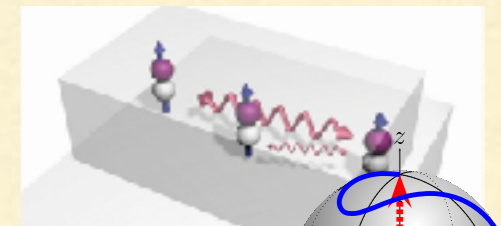
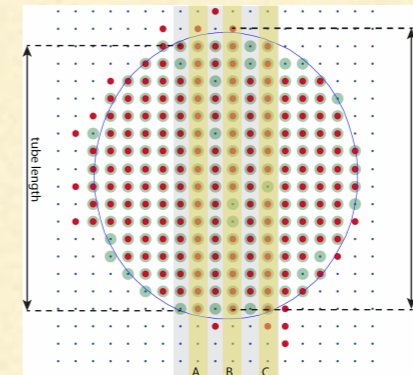
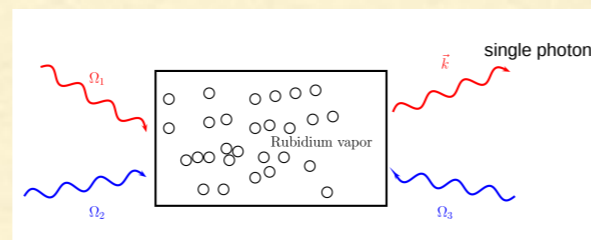
Quantum annealing



Light-harvesting dynamics



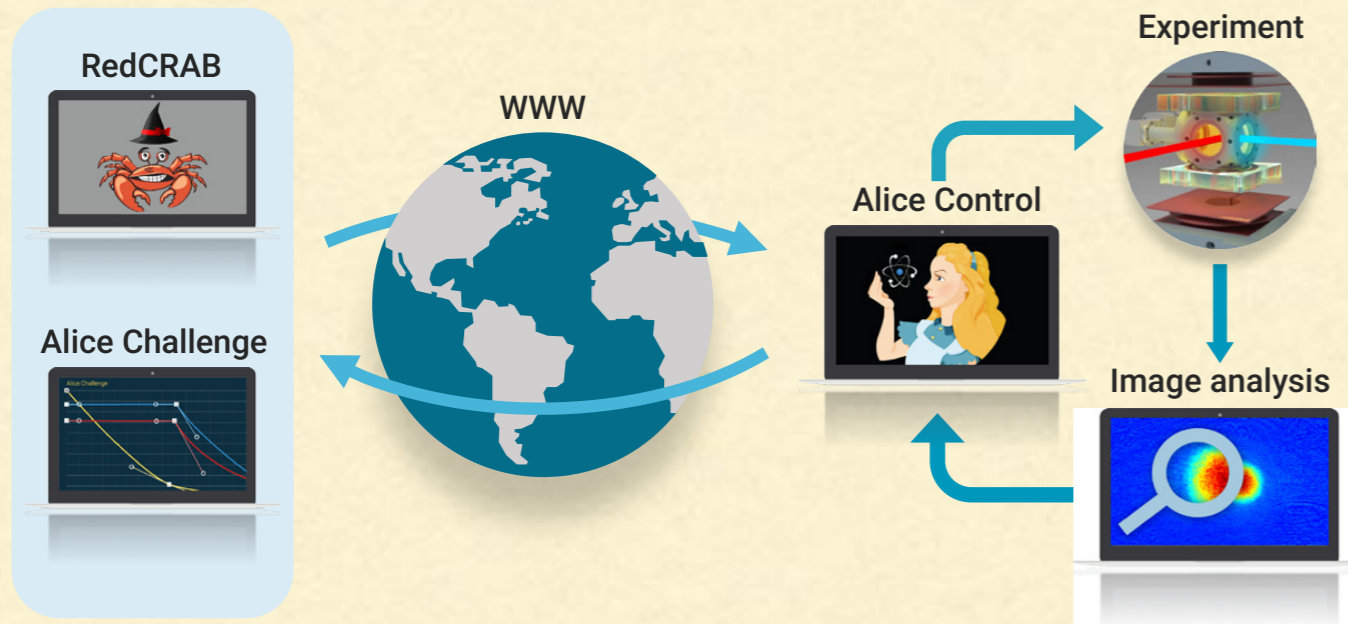
Entanglement/Squeezing manipulation



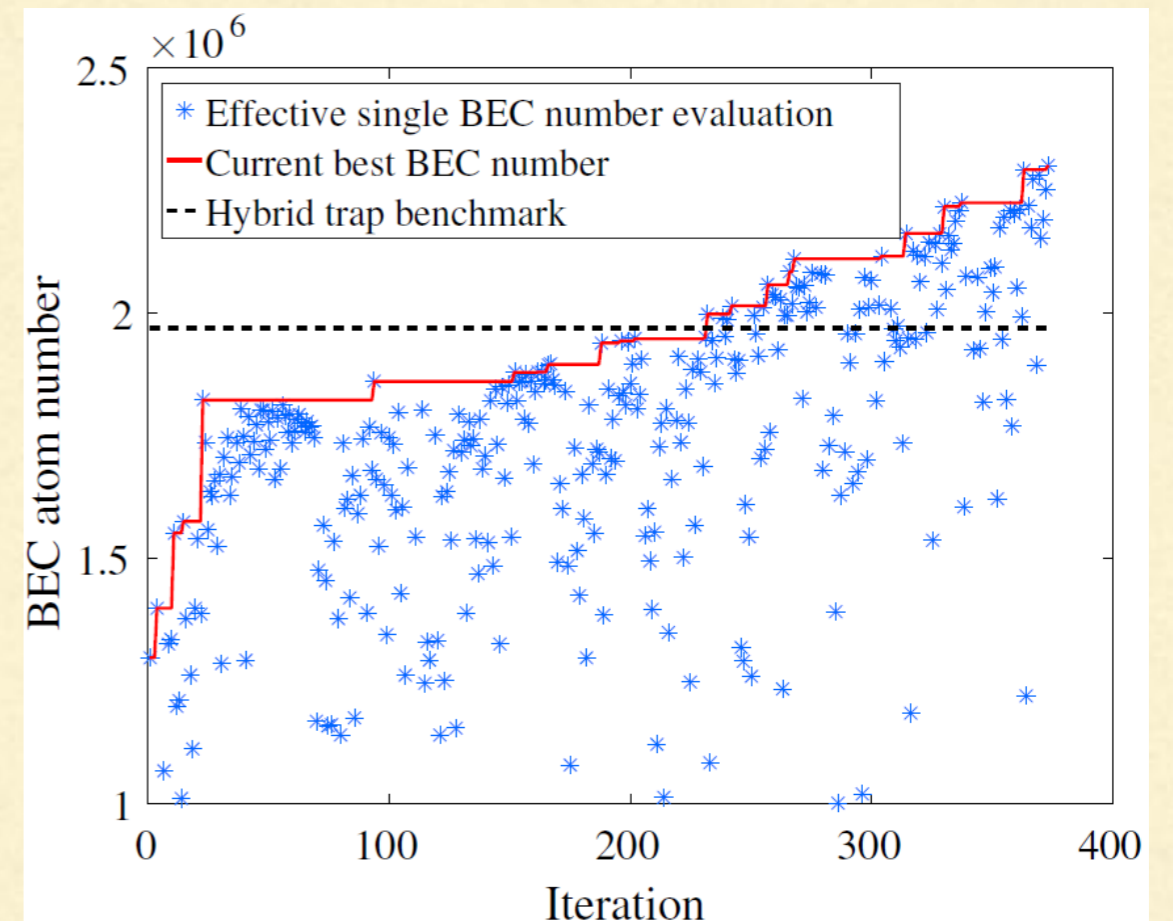
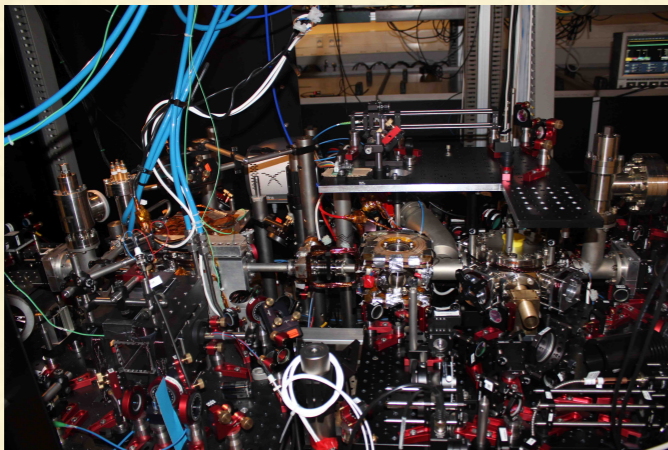
Optimal experimental protocols

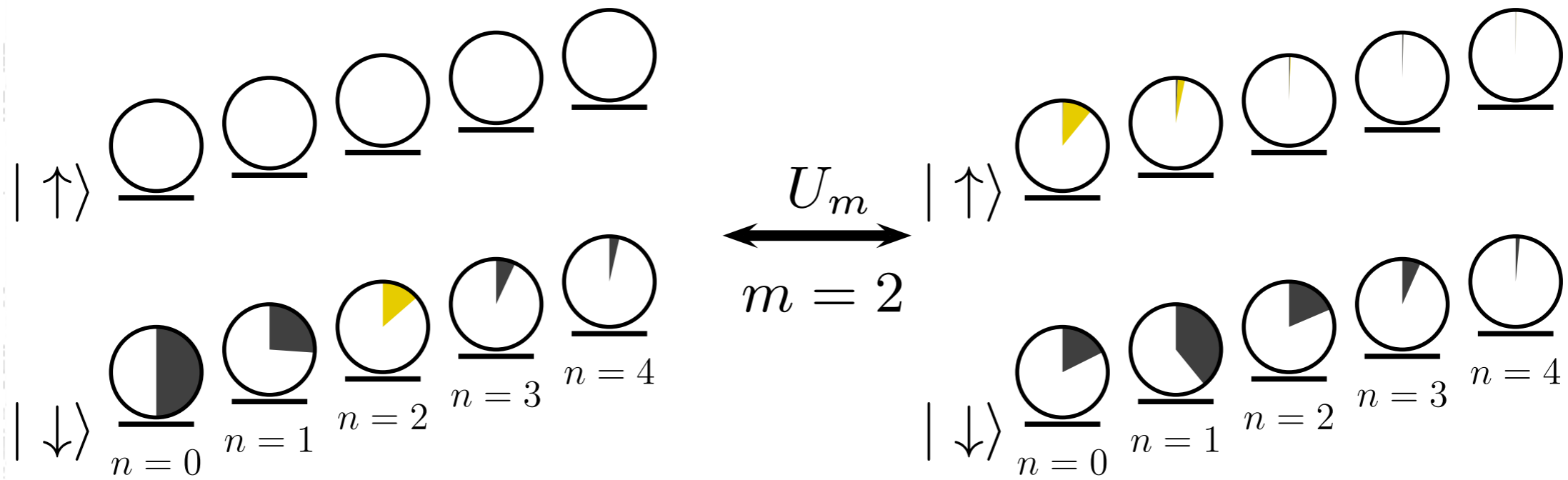
RED CRAB

Server is online!



Maximize BEC atom number





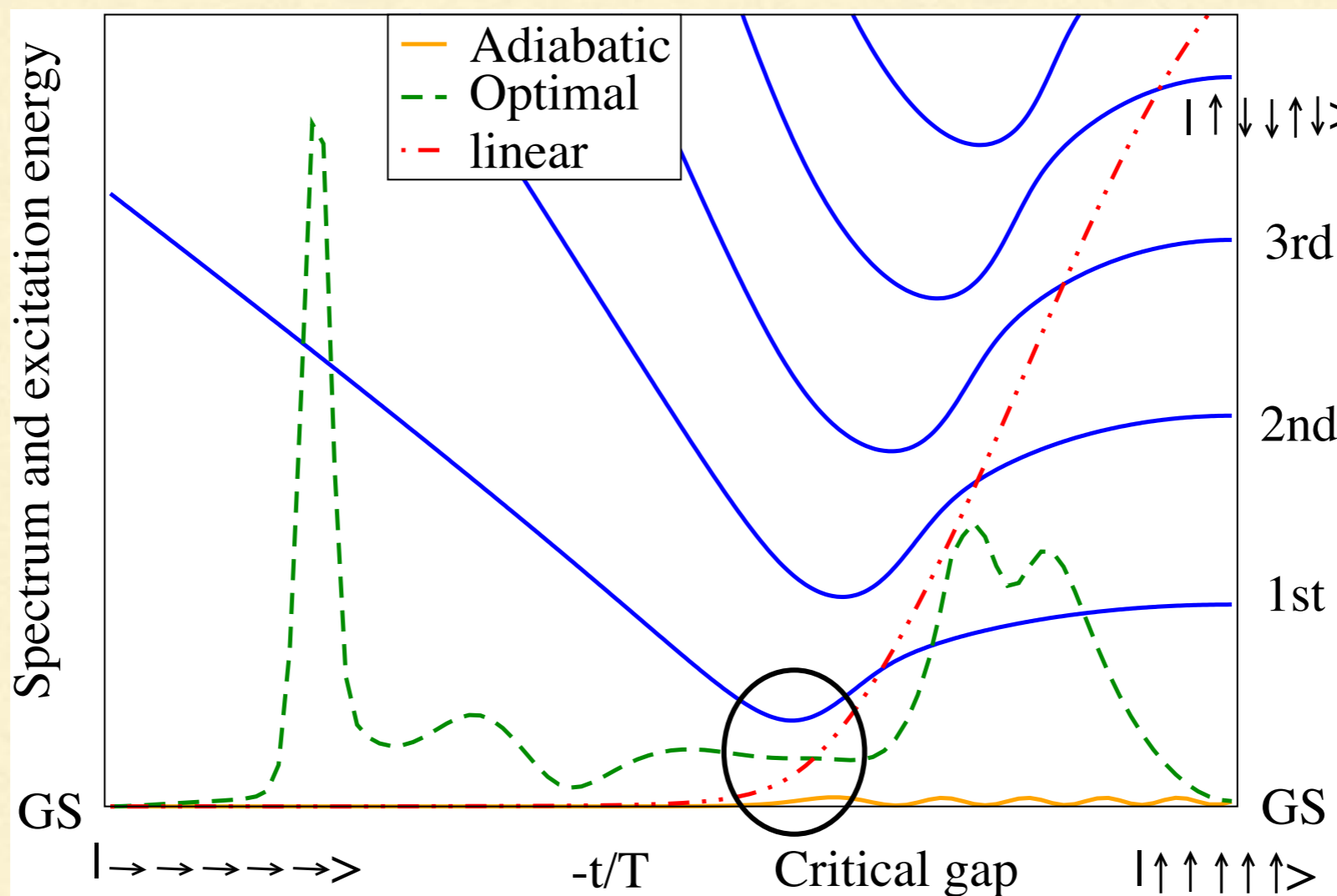
OPTIMAL EXPERIMENTAL PROTOCOLS

Cold atoms in optical lattices, Bose-Einstein condensates on atom chip, NV-centers in diamonds, Rydberg atoms, circuit QED, Trapped ions, Light-harvesting complexes...

OPTIMAL QPT CROSSING

Slow

Fast

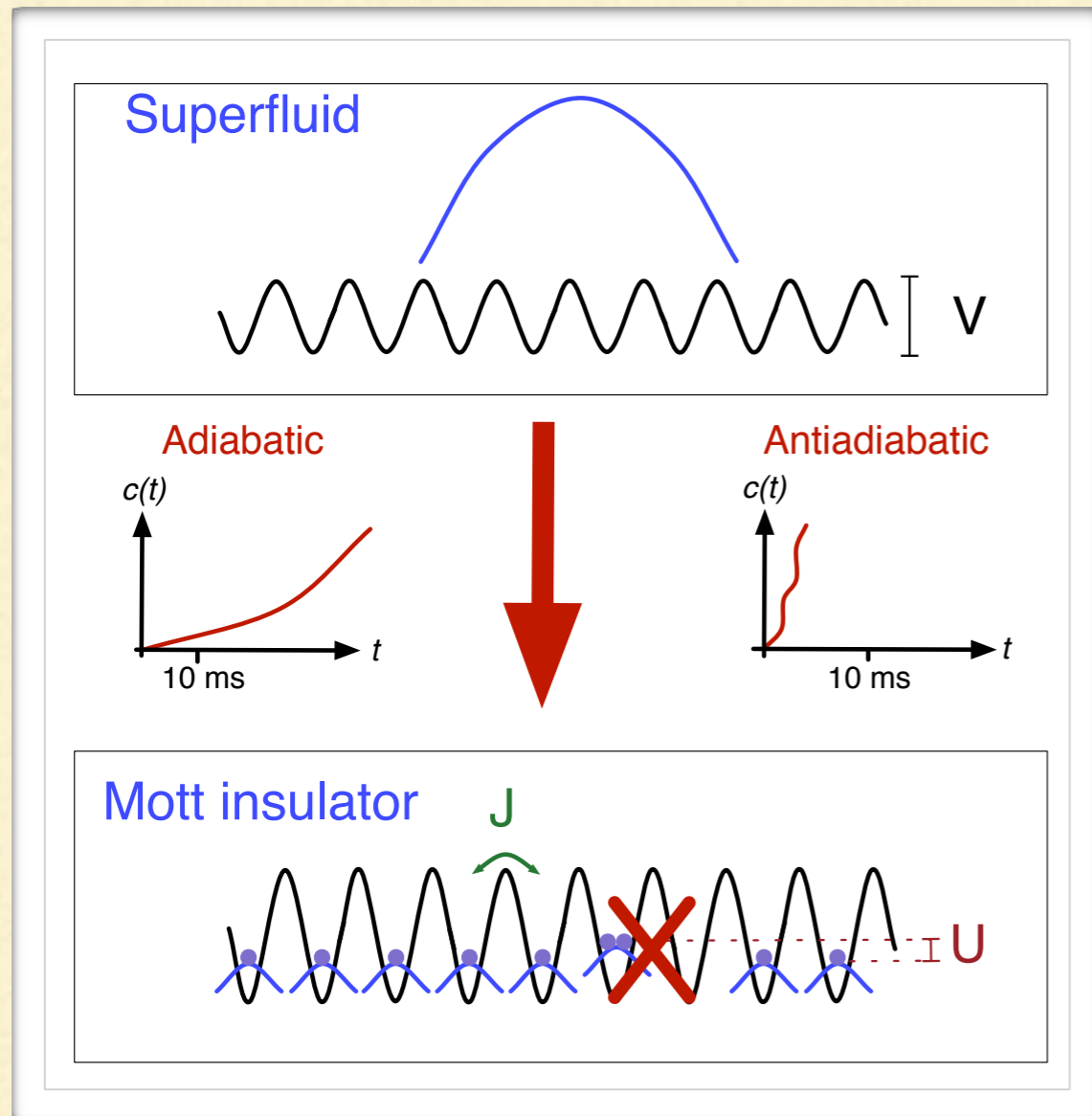


Adiabatic
category

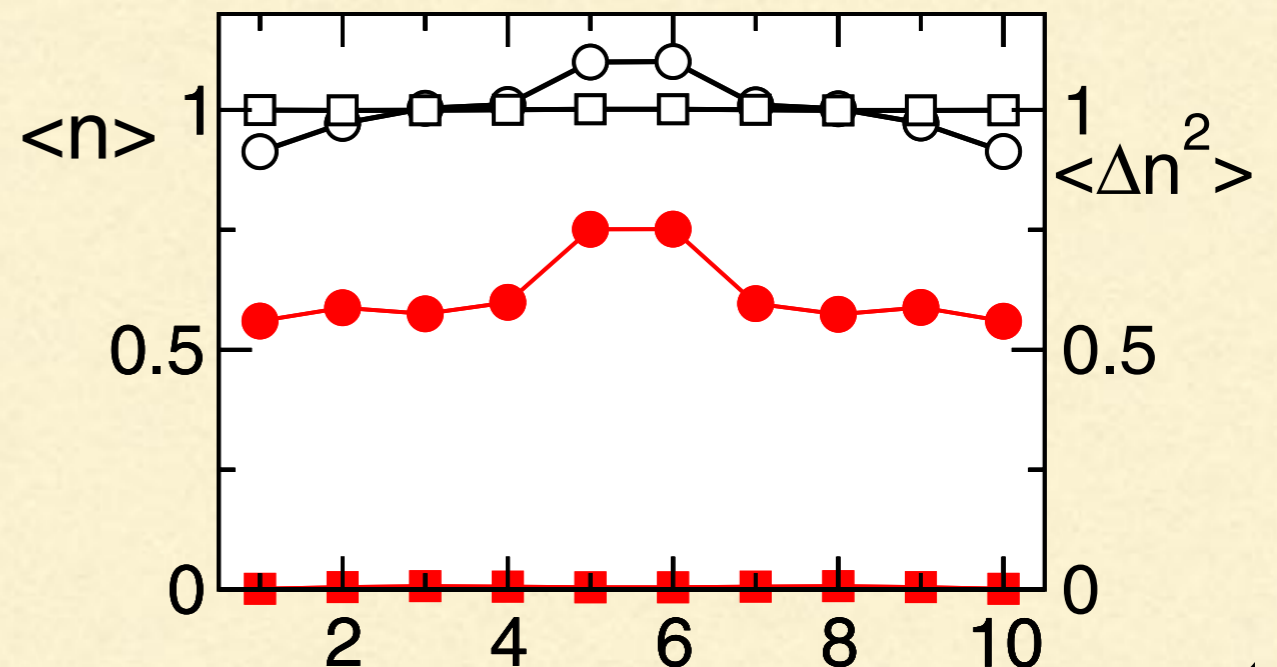
Optimal
control

$$H = -\frac{J}{N} \sum_{i < j} (\sigma_i^x \sigma_j^x + \gamma \sigma_i^y \sigma_j^y) - \Gamma(t) \sum_i \sigma_i^z$$

SUPERFLUID-MOTT INS. QPT

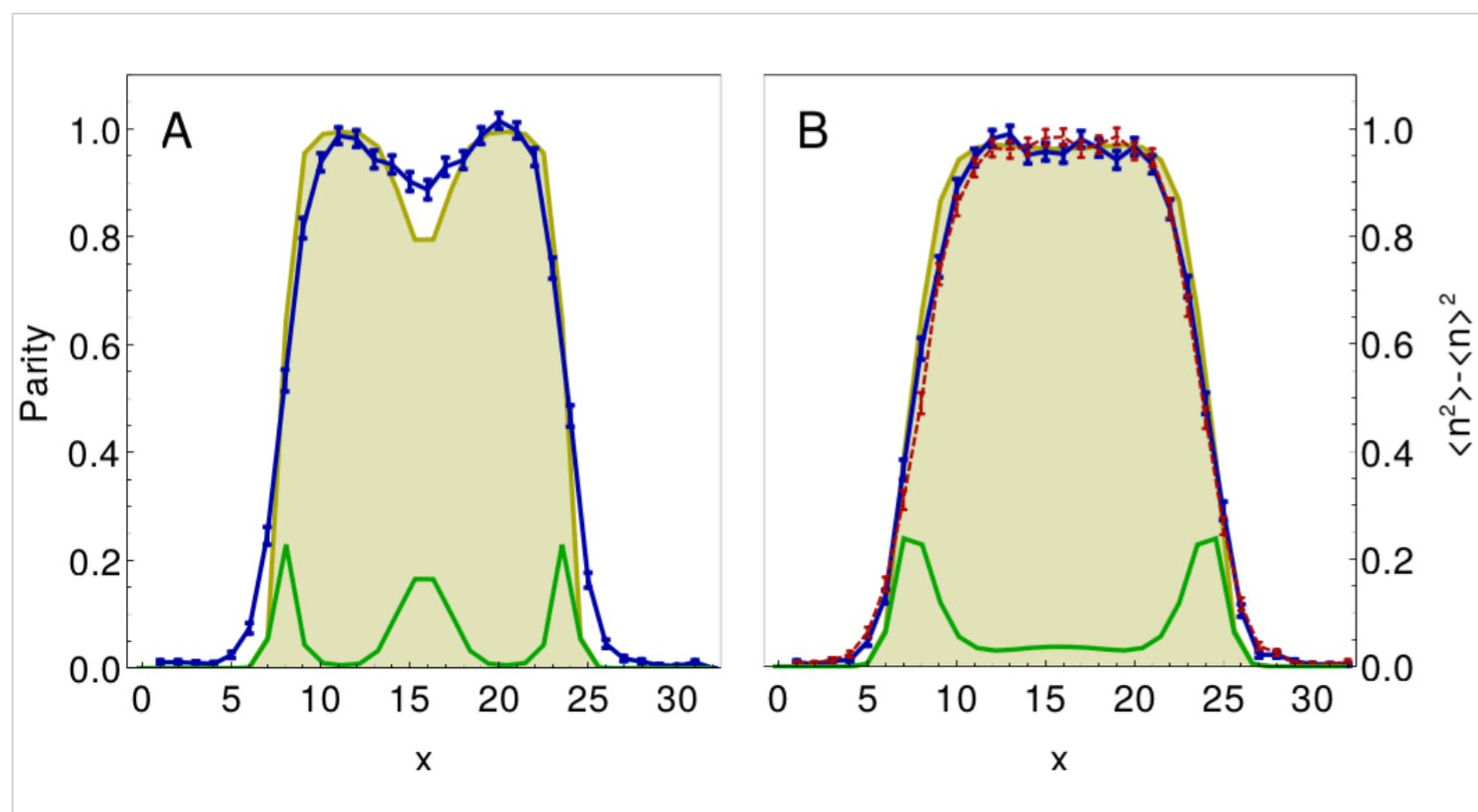


Optimal loading of cold atoms in optical lattices



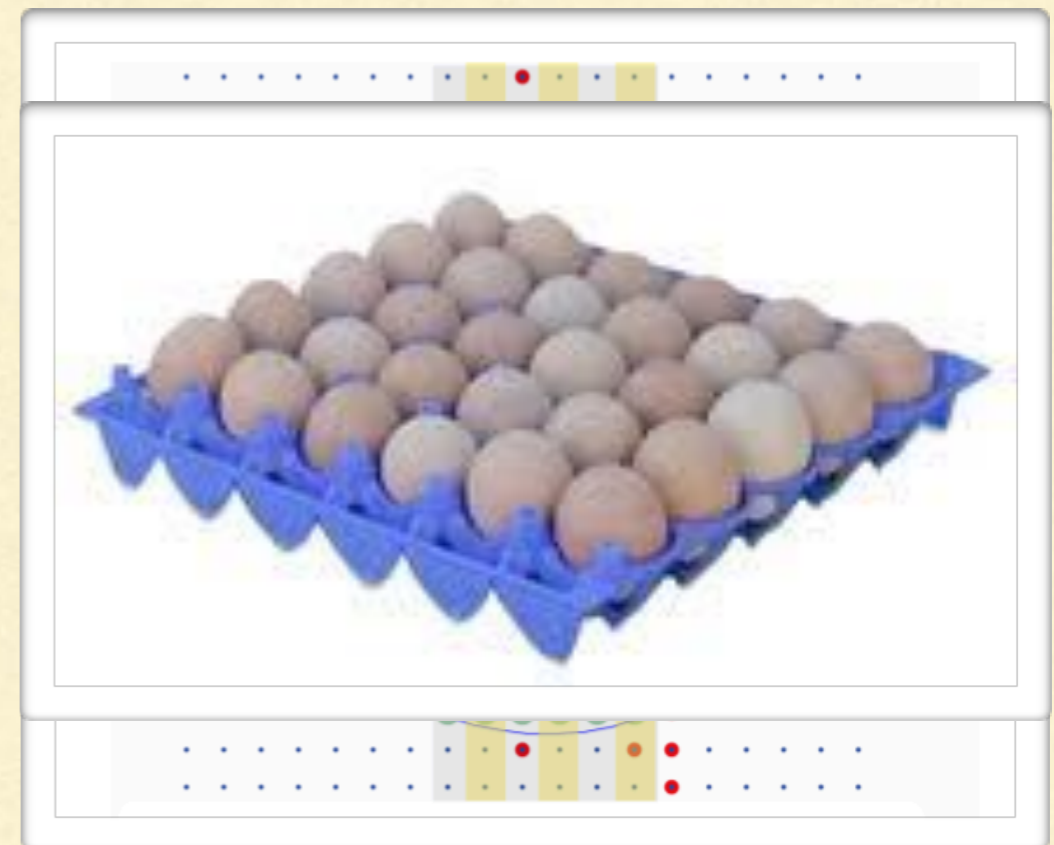
Bose-Hubbard model with external trapping potential

Parity density profiles



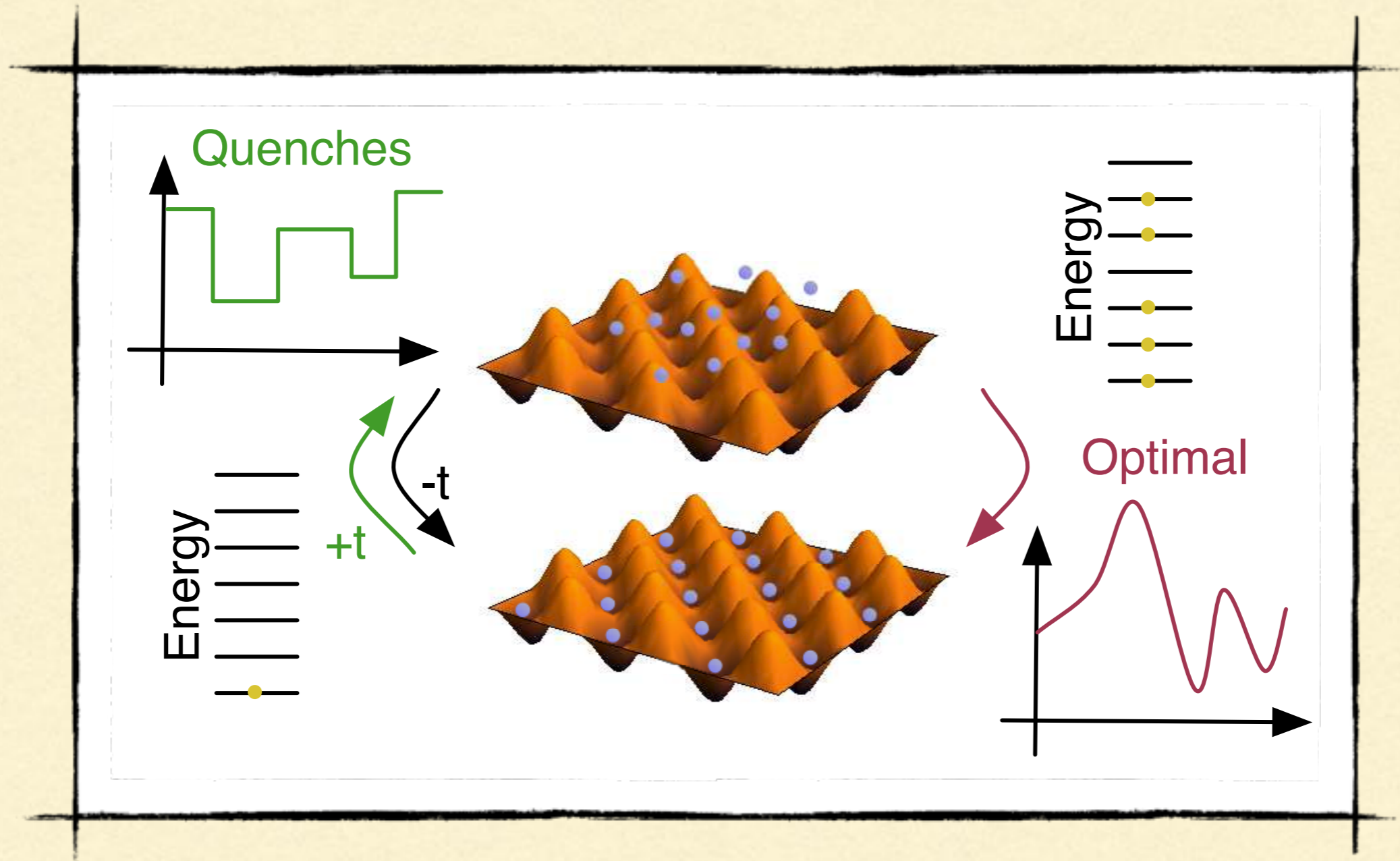
I. Bloch's
group (MPQ-Munich)

One dimensional tubes



EXPERIMENTAL RESULTS

Speed up of one order of magnitude
Compatible with the quantum speed limit



FUNDAMENTAL LIMITS AND COMPLEXITY

Where no man has gone before

PHYSICAL LIMITS

- Reachability

Directions available

- Energy

Power available

- Information

Channel capacity

- Dynamical Lie algebra

$$V^{(0)} \equiv [[iH'_0, iH_1], iH'_0]$$

$$V^{(\ell-1)} \equiv \hat{=} [[iH'_0, V^{(\ell-2)}], iH'_0] - \omega_1^2 V^{(\ell-2)}$$

- Energy-time uncertainty

$$\Delta E \Delta t \geq \hbar/2$$

- Shannon-Hartley theorem

$$k_s = \log(1 + \mathcal{S})$$

OPTIMAL CONTROL COMPLEXITY

- The (smoothed) complexity of an optimal control problem scales **polynomially** with the size of (time-polynomial) reachable states $D_{\mathcal{W}+}$
- Efficiently simulatable dynamics (Integrable, TN, DMFT, HF-like, etc...) can be efficiently optimally controlled
- Final error scales exponentially with the optimal control bandwidth

$$\varepsilon \geq 2^{-\frac{T \Delta \Omega \kappa_S}{D_{\mathcal{W}+}}}$$

- The optimal control bandwidth, total time and the size of the set of reachable states are such that:

TAKE HOME MESSAGES

- Tensor network algorithms field of application is rapidly expanding
 - What can be simulated can be controlled
 - A large class of “complex quantum systems” can be efficiently characterized, simulated and controlled.
 - We aim to support the development of quantum technologies and to study novel interesting phenomena
-



OUTLOOK

Every journey begins with a single step

OPEN QUESTIONS

- New tools and algorithms to simulate quantum systems
 - Software engineering and optimization
 - New protocols for quantum technologies
 - Fundamental limits
 - Classical versus quantum annealing
 - Quantum advantage definition
 - Universal quantum computers?
 - ...
-

VISION

Extreme simulations
of quantum technologies

Software
development

System
modelling

Algorithm

Quantum
mechanics

Computer
science

Physics

NECESSARY KNOW-HOW

- Algorithms
 - Software engineering
 - Complexity theory
 - Graph theory
 - Optimization
 - High performance computing
 - ...
 - Quantum information theory
 - Many-body quantum systems
 - Quantum hardware
 - Tensor networks
 - Optimal control
 - Parallel computations
 - ...
-

OPTIMAL ENGINEERING OF COMPLEX QUANTUM PHENOMENA



- Dynamics of quantum phase transition
- Optimal driving of correlated matter
- Quantum chemistry
- Quantum transport
- Quantum thermodynamics
- Quantum technologies: sensing (NV-centers, graphene nano-ribbons), Quantum simulations (of LGT)...

Thank you for your attention!

Simone Montangero
Mario Collura



Tommaso Calarco
Pietro Silvi
Ressa Said



Thomas Pichler
Tommaso Caneva
Matthias Gerster
Ferdinand Tschirsich
Werner Weiss
Jonathan Zoller
Fedor Jelezko
Boris Naydenov



Matteo Rizzi



Tilman Pfau



S. Lloyd



Peter Zoller
Wolfgang Lechner
Marcello Dalmonte



Enrique Rico Ortega



Rosario Fazio



Jacob Sherson



Immanuel Bloch
Marc Cheneau
Sebastian Hild



Alessandro Silva
Giuseppe Santoro



Jörg Schmiedmayer
Thorsten Schumm
Sandrine van Frank



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QUANTERA
QTFLAG
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Numerics:



New Trends in Complex Quantum Systems Dynamics

9-12 April 2019

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Submit a talk or poster

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| Jilanshu Cao Massachusetts Institute of Technology | Juan José García Ripoll CSIC - Spanish National Research Council | John Coillie Trinity College Dublin |
| Marcus Huber University of Vienna | Genschen Kurtski Vietnam Institute of Science | Misha Lukin Harvard University |
| Martin Plenio Ulm University | Guido Pupillo Strasbourg University | Jörg Schmiedmayer TU Vienna |
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