

# Discrete Biological Models (Modelli Biologici Discreti)

**Zsuzsanna Lipták**

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Università di Verona

Lecture 1 (1 Oct. 2014)

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## What is a discrete biological model?

- **model**: a simplified description, esp. a mathematical one, of a system or process, to assist calculations and predictions  
- Oxford Dictionary
- So **biological modeling** is the act of translating a phenomenon from biology into mathematical language. This allows us to apply known methods to the original problem.
- Note that modeling always involves **simplification**.

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## Modeling molecules as strings



...AACAGTACCATGCTA...  
...TTGTCATGGTACGAT...



...SLDILRRKSLMNYWL...

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## What is a **discrete** biological model?

Uses discrete mathematics:

- natural numbers  $\mathbf{N} = \{0, 1, 2, 3, \dots\}$  or integers  $\mathbf{Z} = \{\dots, -3, -2, -1, 0, 1, 2, 3, \dots\}$
- graphs, trees
- permutations
- strings/sequences
- combinatorics (counting, enumerating a finite number of discrete objects)

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## Example 1: Shotgun-Sequencing of the human genome

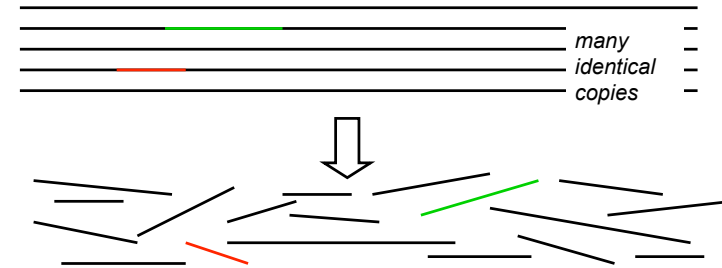


...AACAGTACCATGCTAGGTCAATCGAG...  
 ...TTGTCATGGTACGATCCAGTTAGCTC...

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## Ex 1: Shotgun-Sequencing

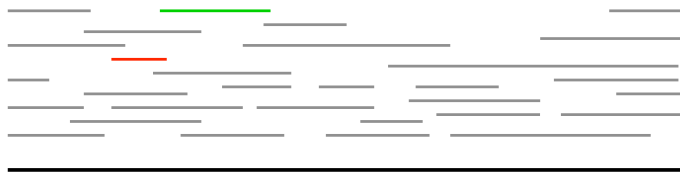
- typical DNA-molecules are several 100'000 bp's long, but only pieces of length 200-700 can be sequenced (Sanger)
- use shotgun-method



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## Shotgun-Sequencing (2)

**Goal:** Reconstruct original string



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## Shotgun-Sequencing (3)

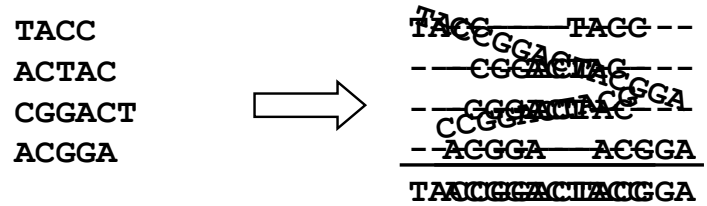
an example:

ACCGT		--ACCGT--
CGTGC		----CGTGC
TTAC		TTAC-----
TACCGT	→	<u>-TACCGT-</u>
		<u>TTACCGTGC</u>

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# Shotgun-Sequencing (4)

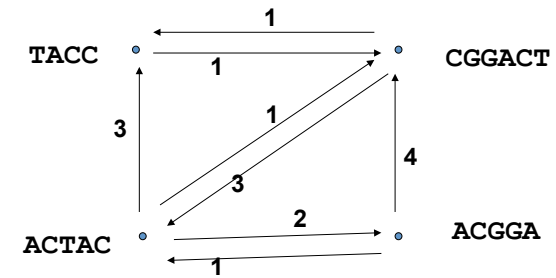
another example:



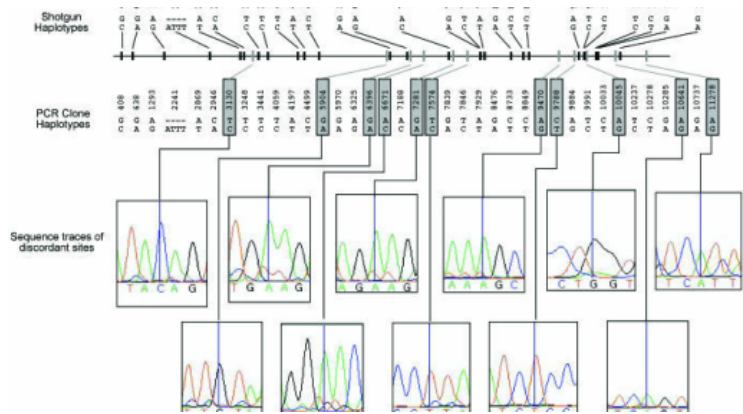
Which solution is better?  
How can we find all solutions?

# Shotgun-Sequencing: Model

overlap-graph (directed, weighted graph):



# Example 2: Haplotyping



# Example 2: Haplotyping

- SNPs (single nucleotide polymorphisms)

0	1	1	0	0	1	haplotype
0	0	1	1	0	1	haplotype
						genotype
0	2	1	2	0	1	
0	1	1	1	0	1	
0	0	1	0	0	1	
0	2	1	2	0	1	

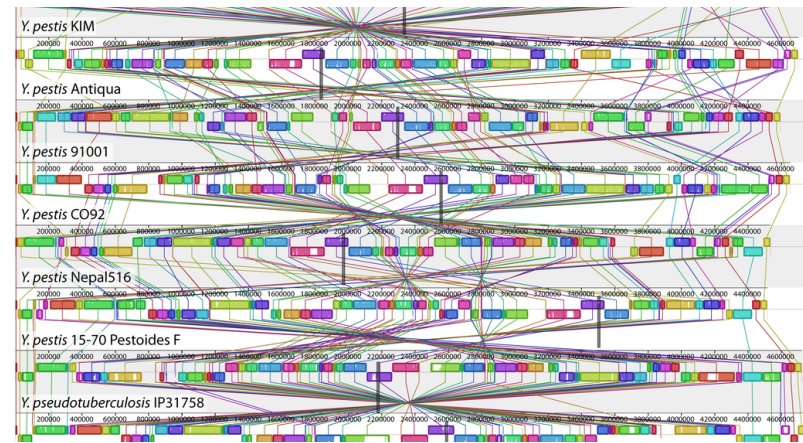
## Example 2: Haplotyping

- given: n genotypes (n individuals)
- find: fewest possible haplotypes that explain the genotypes

02120	22110	20120	→	00100	01110	10110	00100	01110
							<u>01110</u>	<u>10110</u>
							02120	22110
							00100	
							<u>10110</u>	
							20120	

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## Example 3: genome rearrangements



© Darling, Miklós, Ragan

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## Ex. 3: genome rearrangements (2)

human	1 2 3 4 5 6	(gene 1, gene 2, ...)
	↑	how do we get from mouse to human?
mouse	1 3 4 6 5 2	

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## Ex. 3: genome rearrangements (3)

human	1 <u>2</u> 3 4 5 6	(gene 1, gene 2, ...)
	1 3 <u>2</u> 4 5 6	
	1 3 4 <u>2</u> 5 6	
mouse	1 3 4 6 5 2	

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### Ex. 3: genome rearrangements (4)

- **given:** a permutation of  $\{1,2,\dots,n\}$
- **find:** fewest number of reversals to get to the identity permutation

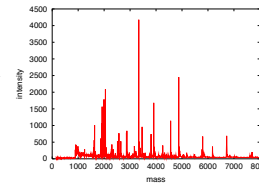
1 3 4 6 5 2  $\longrightarrow$  1 2 3 4 5 6

**(“Sorting by reversals”)**

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### Example 4: Mass decomposition

**mass spectrometry:**



AARLSTRACLSAAIS...  
 LSESMFGHEESLR...  
 SRILSRLELPSGILGG...  
 QEKLHGEEALPSK...  
 ECDNRAALIGRSEDV...  
 ...

*unknown molecular mixture*

*mass spectrum*

*identification*

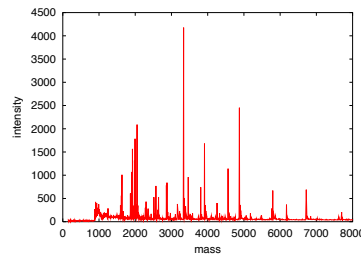
*(DNA, protein, metabolites...)*

*(names, sequences, data base identifiers, molecular structure...)*

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### Ex. 4: Mass decomposition (2)

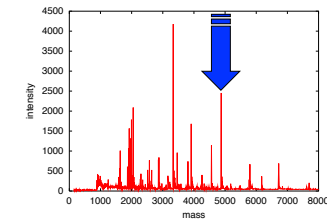
- **input:** unknown molecular mixture (sample)
- **output:** list of masses of the sample molecules (mass in Da, intensity)  
actually:  $m/z$  = mass over charge
- **intensity** proportional to abundance: how often that mass was measured (ideally!)



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### Ex. 4: Mass decomposition (3)

- **Given:** query mass  $M$  (in Da)
- **Known:** What type of molecules are in sample? (DNA, protein, ...)
- **Question:** What molecules can have this mass?



amino acids ( $k = 20$ )		nucleotides ( $k = 4$ )		“bioatoms” ( $k = 6$ )			
Ala (A)	71.079 Da	A	313.058	C	12.0	O	15.995
Arg (R)	156.101	C	289.046	H	1.008	P	30.074
Asn (N)	114.043	G	329.053	N	14.003	S	31.972
...		T	304.046				

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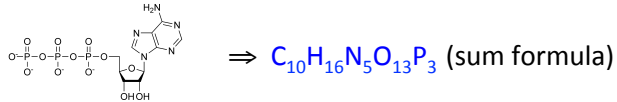
## Ex. 4: Mass decomposition (4)

NB:

- output will be: **composition/sum formula** (not: sequence or molecular structure!)

EGAEYSSFL  $\Rightarrow A_1E_3G_1L_1F_1S_2Y_1$

AACGTAGGAA  $\Rightarrow A_4C_1G_3T_1$



- take into account **error** (measurement, computation)

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## Ex. 4: Mass decomposition (5)

### Money Changing Problem (MCP):

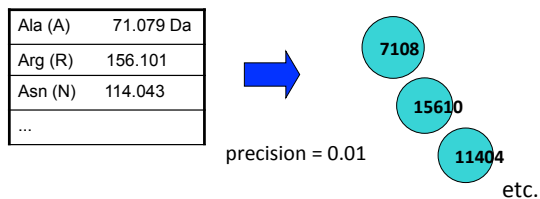
- Given:
  - $k$  coin denominations  $\{4, 5, 7\}$
  - positive integer  $M$
- Question: How can we make change for  $M$ ?

$$19 = 3 \cdot 5 + 1 \cdot 4 = 3 \cdot 4 + 1 \cdot 7 = 2 \cdot 7 + 1 \cdot 5$$

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## Ex. 4: Mass decomposition (6)

Translating the MS problem into MCP:



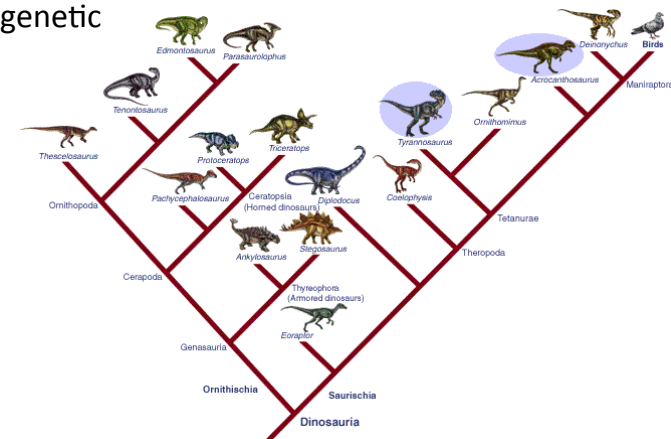
**Given:** query  $M$ , error bound  $\epsilon$ .

Compute all decompositions of masses between  $M - \epsilon$  and  $M + \epsilon$  (scaled to integers with factor  $1/\text{precision}$ ).

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## More discrete models in bioinformatics

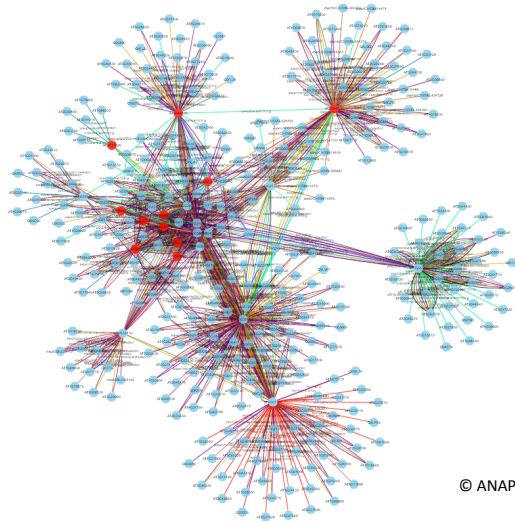
Phylogenetic trees



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## More discrete models in bioinformatics

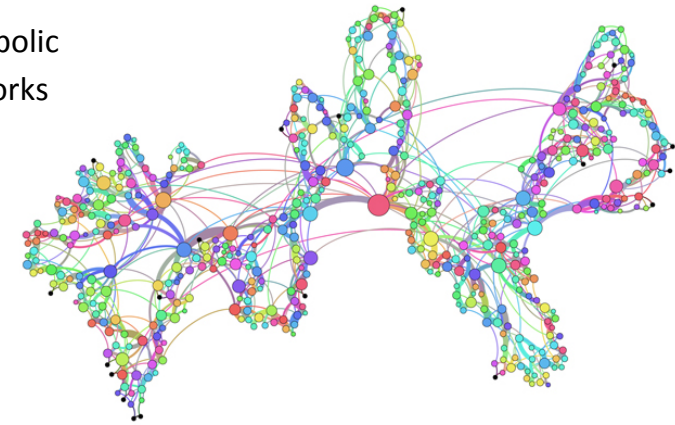
Protein  
interaction  
networks



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## More discrete models in bioinformatics

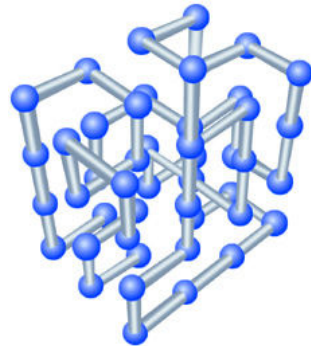
Metabolic  
networks



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## More discrete models in bioinformatics

Discrete models  
for protein folding  
(H-P model)



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## More discrete models in bioinformatics

and, and, and ...

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End of introduction.  
Now it's time to start working.